

Evaluation of Liquid Film Thickness in Gas-Liquid Annular Flow in Horizontal Pipes Using Three Methods

Osokogwu Uche

Oil & Gas Engineering Centre, Cranfield University, Bedfordshire, UK

Email address:

Oxgoodlt@yahoo.com

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Abstract: Experimental investigations on annular flow film thickness were conducted using a closed-loop horizontal pipe with an internal diameter of 2-inch (0.0504m). The aim is to progress the understanding of such flow and facilitate the optimum design of hydrocarbon production systems where such flow is encountered. Liquid film thickness was extensively investigated using three methods: the conductance probe sensors installed at the bottom of the pipe, conductivity ring sensors and triangular relationship model. From these methods, liquid film thickness was proven to decrease with increase in superficial gas velocity, while increases with increase in superficial liquid velocity. In comparison, the predicted triangular relationship liquid film thickness matched better with the liquid film thickness obtained from conductance probe sensors at all the flow conditions in the experiments, while the conductivity ring sensor results matched closely at superficial liquid velocity of 0.0505m/s and 0.0714m/s but overestimated at superficial liquid velocity of 0.0903m/s and 0.1851m/s. This has shown the impact of high superficial gas velocity on conductivity ring sensors in accounting for liquid film thickness.

Keywords: Film Thickness, Gas Velocity, Annular Flow, Sensors, Liquid Entrainment, Flow Rate

1. Introduction

Multiphase flow in pipes involve different phases flowing together, either at the same or different velocity. As the flow develops along vertical or horizontal pipes, different flow patterns or flow regimes could be observed, depending on the dominant phase in the system, properties of each phase in the flow (e.g. viscosity, density) its velocity and pipe geometry. The focus here is on annular flow, which is a complex flow regime encountered in horizontal and vertical pipes in the oil and gas industry, [14]. Gas-liquid annular flow is also encountered in nuclear power plants, chemical and refining processes like reactors, heat exchangers.

Annular flow in horizontal pipes flow with much gas velocity at the core centre of the pipe with impact of gravity leaving the circumferential liquid film on the internal walls of the pipe which drains to the bottom of the pipe as film thickness, [15]. According to [19], the liquid flows as a film along the pipe walls under gravity, induced by the high velocity gas stream in the pipe core. The gas together with entrained liquid droplets, flows within the core of the pipe; at high velocity the entrained droplets travel at a velocity close

to that of the gas, [8]. Annular flow represents a thick liquid film at the bottom that moves slowly on the internal pipe walls than the gas phase, [8]. The combined slow flow of the liquid at the bottom with the fast gas phase at the interface, aids to increase the pressure gradient and wall shear stress in annular flow. However, a thin liquid film exists at the curved surfaces and the upper walls while a thick liquid film exists at the bottom of the internal diameter of horizontal pipes, [14]. More so, the liquid which is non-uniform flows circumferentially around the pipe walls. According to [20], the asymmetry distribution of annular flow in horizontal pipes is dependent on the mass flow rate of the liquid and gas. Liquid film thickness is observed to be higher at the bottom of the pipe compared to the curved surface area and the upper walls of the pipe internally. This is because of the effects of gravity-induced drainage, which increases the liquid film thickness at the bottom of the pipe, [20, 21]. Also, [13] investigated and reported on circumferential water film thickness in annular in pipes, [1] presented film thickness at the upper part of the walls of the pipe while [2] conducted experiments on film thickness with respect to axial flow. [3, 22, 9, 18] likewise investigated liquid film thickness in

annular flow in pipes.

In determining liquid film thickness in the pipes, the fraction of liquid droplets dispersed in the gas core are accounted while the film thickness at the walls of the pipes is measured using any of the following techniques: *optical techniques*: e.g. pin, high speed cameras/Laser for detecting interface, *electrical techniques*: capacitance, conductance method (flush-mounted, parallel-wire), *acoustic techniques*: e.g. ultrasonic in which the reflected signals of time interval emitted from gas-liquid interface are converted to film thickness, and the *radiological techniques*: e.g. X-ray, neutrons and gamma-ray. The radiological techniques use different attenuations to measure liquid film thickness in the pipes. The above techniques differ in measurement principles, ease of use, frequency response, calibration techniques, accuracy and method of installation (intrusive or non-intrusively mounted) and ease of data extractions/analysis.

For the liquid droplets dispersed in the gas core, it involves a droplet-breakup from the liquid film due to wave actions of the high gas velocity flow in the pipes. Entrainments in gas core have been investigated with wide publications. Among the experimental investigations on entrainment in horizontal pipes are: [23] who presented an entrainment correlation group R (lbmft³/lbf-hr) which was developed based on pipe internal diameters of 25.4mm and 76.2mm with superficial liquid velocities of 0.12-0.77m/s and superficial gas velocities of 12- 62m/s. Again, critical Weber number ranging from 13 to 22 and pressure gradient, were considered in the correlation expressed as:

$$R = \left(\frac{q_L}{q_g} \right) \left(\frac{N_{WeCr} W_{LE}}{(dp/dL)_G} \right) \quad (1)$$

The above equation (1) of the entrainment correlation group R could be re-written with Lockhart-Martinelli parameter X , if the correlation group R is within the ranges of 0.5 to 200.

$$R = 168X^{2.05} \quad (2)$$

while,

$$X = \sqrt{\frac{(dp/dL)_L}{(dp/dL)_G}} \quad (3)$$

Correlation on gas velocity, viscosity, droplet concentration, surface tension and liquid density was presented by [16]. The correlation is expressed as:

$$F_E = 0.015 + 0.44 \log \left[\frac{\rho_m}{\rho_L} \left(\frac{\mu_{LV}^2}{\sigma} \right) 10^4 \right] \quad (4)$$

More so, [5], developed their correlation based on air/water flow using a 0.0231m pipe diameter. The flow conditions considered in their correlation were based on V_{sg} of 15-88m/s, V_{sl} of 0.0072-0.9m/s, gas density (between 1.6 to 2.75kg/m³), liquid density of 1000kg/m³ with liquid viscosity of 1mPas and surface tension of 73mN/m. The developed correlation is

$$\dot{\epsilon} = K_A \left(\frac{W_{LF} - W_{LFC}}{P} \right) V_g^2 \rho_g^{0.5} \rho_f^{0.5} \quad (5)$$

where,

$$K_A = 3.5 \times 10^{-6} \frac{sec^2}{kg} \quad (6)$$

and;

$$\frac{W_{LFC}}{P} = 0.046, \frac{kg}{m.s} \quad (7)$$

The correlation considered a pipe with an internal diameter of 0.0231m.

An explicit correlation that considers critical liquid film rate was reported by [17]. The correlation considers deposition coefficient, droplet size, entrainment fraction, maximum entrainment as noted by [12, 10]. Below is the correlation:

$$\frac{f_E / f_{Em}}{1 - f_E / f_{Em}} = 9 \times 10^{-8} \left(\frac{D v_{g \sqrt{\rho_L - \rho_g}}^3}{\sigma v d} \right) \quad (8)$$

where,

$$f_{Em} = 1 - \frac{W_{FCr}}{W_L} \quad (9)$$

Where critical liquid-film-flow rate could be calculated using:

$$W_{FCr} = 0.25 \mu_L \pi D R_{eFCr} \quad (10)$$

While the Reynolds number for liquid-film-flow rate is:

$$R_{eFCr} = 7.3(\log \omega)^3 + 44.2(\log \omega)^2 - 263 \log \omega + 439 \quad (11)$$

and,

$$\omega = \left(\frac{\mu_L}{\mu_g} \right) \sqrt{\frac{\rho_g}{\rho_L}} \quad (12)$$

The limitation of this correlation is that, critical-film-flow rate gives a negative result on maximum fraction of entrainment for low liquid flow rates.

Also, [12] developed correlations for entrainment fraction and maximum entrainment based on pipe diameters of 50.8mm and 152.4mm (ID). In the developed correlations, superficial liquid and gas velocities, pipe diameter, liquid wave, deposition coefficient and wave fraction were considered. The entrainment fraction correlation is as follows:

$$f_E = \frac{1 - \frac{4}{V_{SL} \pi D^2} \int_0^{A(A_{Lh})} u dA}{1 + \frac{K_g}{V_{SG}} \frac{4 S_L W}{\phi \pi D^2}} \quad (13)$$

while the maximum entrainment correlation is here below:

$$f_{Em} = 1 - \frac{q_{FCr}}{q_L} \quad (14)$$

where the critical liquid film flow rate is given as:

$$q_{fcr} = \pi D v (12.514 + 5 h_{Lm}^+ \ln h_{Lm}^+ - 8.05 h_{Lm}^+) \quad (15)$$

Where the dimensionless liquid film thickness at maximum entrainment condition is:

$$h_{Lm}^+ = 0.6R_{eSL}^{0.45} \quad (16)$$

The correlations could be improved by introducing frequency, wave celerity, amplitude and spacing [12].

The combination of the entrainment correlation results and the reference film thickness from the conductance probes and conductivity ring sensors' experiments, will yield liquid film thickness in annular flow in pipes. However, the emphasis on this paper is to compare the conductance probes, ring sensors and the triangular relationship in harnessing annular flow

liquid film thickness in horizontal pipes.

2. Material and Methodology

The method involved air/water experiments using a closed loop system pipe of 2-inch (0.0504m, ID) with a total length of 28.68m. The liquid film thickness was measured using *electrical techniques*: conductance method (probes) (flush-mounted) and conductivity ring sensors with the experimental properties and ranges as:

Table 1. Experimental Properties and Ranges Used.

Properties	Range	Units
Temperature	16.5-19.3	°C
Pipe internal diameter (flow loop)	0.0504	m
Air flow line internal diameter	0.0504	m
Superficial liquid velocity	0.0501-0.2001	m/s
Superficial gas velocity	8.0774-23.7260	m/s

The annular flow liquid film thickness results which were obtained using the conductivity ring sensors and conductance probe sensors, were compared with the triangular relationship results.

Experimental Set-Up

The experiments were conducted using a pipe with an internal diameter of 2-inch (0.0504m) at the Process Systems Engineering (PSE) Laboratory, Cranfield University. The 2-inch (0.0504m) pipeline test facility of 28.68m was a closed-loop system, where water inlet pipe was connected to the water tank and the outlet was also connected back to the same storage water tank. On the flow loop were, 2 pairs of pressure transducers (Druck) with the upstream (T1) as (PMP 4070, S/N 2642126) and downstream (T2) as (PMP 4070, S/N 2630077) which were installed at 2.08m apart from one another. The essence of the difference was to observe the pressure behave immediately after the gas and sand entry points and the multiphase flow behavior after symmetrically distribution of the fluids in the experiments. Other instruments installed were: light emission diode infrared sensor (LED), conductivity ring sensors of double pairs installed at 0.07m apart and two set of conductance probes also installed at 0.20m apart on the flow loop as shown in Figure 1. The air-line which was a 2-inch (0.0504m) has a delivery capacity of superficial gas velocity of 30m/s with air flowmeter, pressure transducers and temperature sensors also connected to it. The sand injection point to the sand sampling location (point) was 5.27m, while the sand injection point to the upstream conductance probe (S1) was 2.39m and to second probe downstream (S2) was 2.59m.

During the experiments, the water line is often open to flow to stabilize before the gas line through the second valve before the vortex air flowmeter. The air supplies were meter and the pressure similarly recorded with P_g while the temperature, also recorded as T1. These instruments were, connected to a LabVIEW where the data were recorded.

From Figure 1, is the sketch of the 2-inch (0.0504m) pipe flow loop, with the instruments/lines representing the colors follows: The Red Line: is for gas supply, the Blue Line: is for water supply, the Pink Line: represents the multiphase flow, while the Green Line: is for sand/water mixture (slurry flow) from the sand hopper.

Mechanism of Sensors used for Film Thickness.

The two sensors used in the determining liquid film thickness are conductance probe sensors (C1 and C2) and conductivity ring sensors S1 and S2 shown in figure 1.

Conductivity Ring Sensors.

The sensors were two pairs of ring-type sensors that were installed on the outer walls of the 2-inch Plexiglas pipe used. They are used to obtain flow values by injecting electric current into the pipes through the outer pair of electrodes and measuring the corresponding electric potential drop in between each successive electrode [4]. The conductivity ring sensors are used to measure liquid hold up. It measures a resistance based on amount of liquid fraction in the system or pipes and gives an output voltage as its readings. In this study, the rings were equally used for liquid film thickness during the experiments.

Conductivity Probe Sensors

The conductance probe sensors operate based on the conductivity charge caused by conductivity liquid. The sensors when in contact with water, has a potential difference applied to the electrodes. The probe sensors are flush mounted conductance probe sensors consist of two pairs of S1 and S2 which were installed at 0.21m apart on the flow loop as shown in Figure 1. They have a circular conductive plate at the center with a diameter of 10.25mm as well as an outer circular conductive plate of 1.80mm which were duly separated by a 2.40mm circular insulator (see Figure 3). The conductance probe sensors, detect liquid film thickness by recording the output voltage in a digital data acquisition system (LabVIEW).

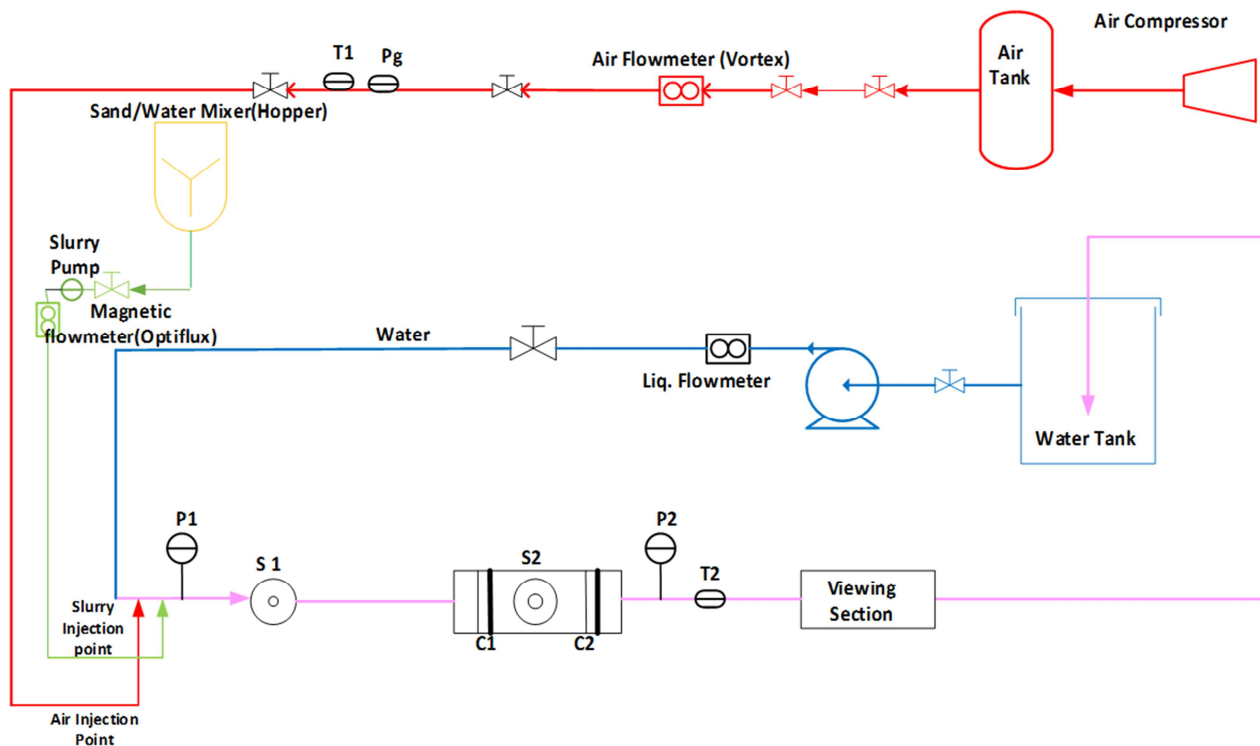


Figure 1. A Sketch of Experimental 2-inch Flow Loop Facility used.

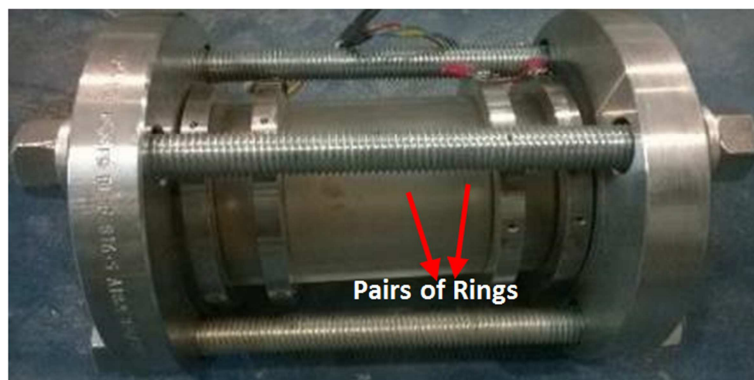


Figure 2. A Typical example of Ring Sensors used.

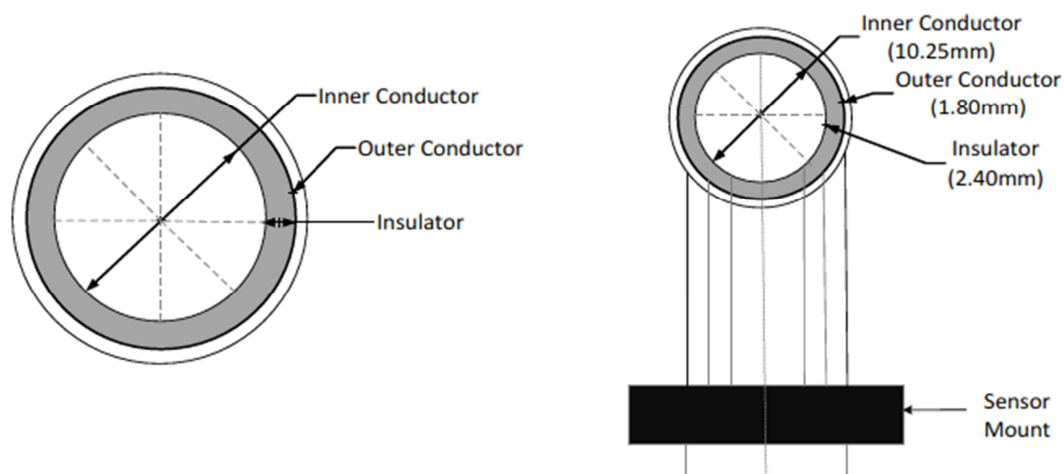


Figure 3. A Sketch of the Sand Probe Sensors Used.

Procedures for determining Film Thickness.

To produce annular flow trend in the experiments, where the superficial gas velocity will be dominant at the core centre of the pipe, bench calibrations were involved. The annular flow bench calibrations were conducted using conductance probe and conductivity ring sensors in a 50mm (0.0504m, I.D) pipe with a length of 170mm. The annular flow bench calibrations were achieved, using five solid cylindrical blocks (plastics) of 49mm, 48mm, 47mm, 46mm and 45mm which were inserted at different times with their voltage recorded. From the bench calibrations, equation (17) was obtained for determining the liquid film thickness as:

$$Y = -0.0044X^2 + 0.1256X + 0.112 \quad (17)$$

3. Result and Discussion

Figure 4, presents the liquid film thickness results. More so, the graph of Figure 4, shows that the liquid film thickness,

decreases with increase in superficial gas velocity, and increases with increase in superficial liquid velocity, as average superficial liquid velocity of 0.0505m/s plot indeed, has the lowest film thickness while the superficial liquid velocity of 0.1851m/s represented the highest film thickness. Again, Figure 4 had also shown that, as the superficial liquid velocity becomes higher, the rate of decrease in film thickness becomes insignificant at the bottom of the pipes. This is because of gravity impact overtime on the break-up droplets. As more of the break-up droplets are lifted, they indeed become heavier and with the impact of gravity, drains to the bottom of the pipes. These mechanisms were also noted by [20, 21]. And for these reasons, the graph of superficial liquid velocity of 0.1851m/s in Figure 4 seems to be a straight line with equal heights across all the superficial gas velocity conditions. However, the heights were not precisely equal as the detailed analyzed results provided in Tables 2-6 proved it.

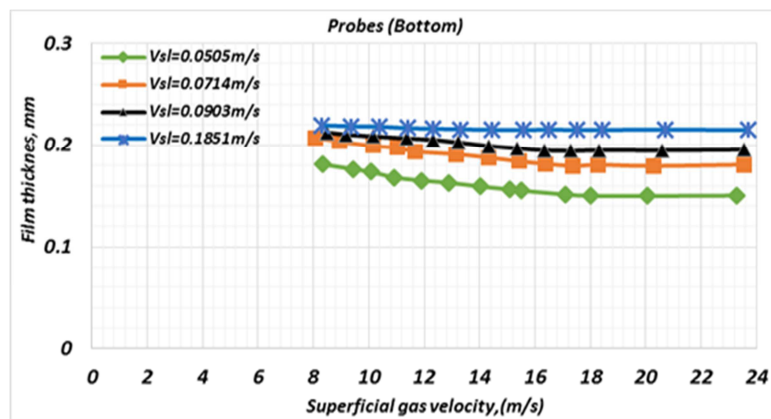


Figure 4. Film thickness (probe at bottom) against superficial gas velocity.

Tables 2-6 are the experimental results of liquid film thickness from conductivity ring sensors, conductance probe sensors and the triangular relationship. The liquid hold-up was obtained from the conductivity ring sensors in the experiments. On liquid entrainment, three correlations

namely; [17, 16] and [11] were accessed but [17] was used. The liquid entrainment results were added to both the liquid film thickness results from conductivity ring and conductance probe sensors as shown in Tables 2-6.

Table 2. Experimental Results for $V_{sl}=0.0505\text{m/s}$ with Liquid Entrainment Correlations.

$V_{sl}=0.0505\text{m/s}$						
	Rings+ Liq Entrain	Probes (Bottom)	Triangular Relationship	Liquid Entrainment Correlations		
HL+Liq Entrain	Film Thickness (mm)	Film Thickness (mm)	Film Thickness	Pan & Hanratty (2002b)	Paleev & Fillippovich (1966)	Mantilla (2008)
0.01805	0.22851	0.18109	0.25404	8.84044E-06	0.011614078	0.000673121
0.01678	0.21238	0.17616	0.22012	1.2937E-05	0.04033245	0.000691296
0.01608	0.20338	0.17360	0.20787	1.56074E-05	0.054660605	0.000697074
0.01484	0.18775	0.16811	0.17948	1.974E-05	0.072768205	0.000694863
0.01454	0.18390	0.16503	0.16571	2.55332E-05	0.092833339	0.000717282
0.01418	0.17928	0.16286	0.15528	3.2343E-05	0.111487851	0.000735483
0.01355	0.17137	0.15922	0.14204	4.15304E-05	0.131456057	0.000748038
0.01306	0.16514	0.15623	0.13006	5.15951E-05	0.148994146	0.000759461
0.01278	0.16160	0.15508	0.12558	5.65125E-05	0.156410786	0.000762028
0.01227	0.15502	0.15137	0.11301	7.42342E-05	0.178847765	0.000777846
0.01203	0.15205	0.15005	0.10861	8.71451E-05	0.192192144	0.000788953
0.01204	0.15216	0.14985	0.10799	0.000120391	0.219445402	0.000827504
0.01224	0.15471	0.15030	0.10767	0.00018716	0.257454679	0.000856896

Table 3. Experimental Results for $V_{sl}=0.0714\text{m/s}$ with Liquid Entrainment Correlations.

$V_{sl}= 0.0714\text{m/s}$						
	Rings+Liq Entrain	Probes (Bottom)	Triangular Relationship	Liquid Entrainment Correlations		
HL+Liq Entrain	Film Thickness (mm)	Film Thickness (mm)	Film Thickness	Pan & Hanratty (2002b)	Paleev & Fillippovich (1966)	Mantilla (2008)
0.02251	0.28528	0.20714	0.26959	8.81788E-06	0.065940703	0.000664107
0.02115	0.26788	0.20362	0.23915	1.25164E-05	0.091332006	0.000681619
0.01957	0.24780	0.19932	0.20482	1.71117E-05	0.114274913	0.000688195
0.01885	0.23868	0.19726	0.18937	2.1732E-05	0.131996775	0.00070105
0.01758	0.22253	0.19364	0.17408	2.56301E-05	0.144327877	0.0006918
0.01649	0.20864	0.19096	0.16061	3.63006E-05	0.170623647	0.000704438
0.01538	0.19452	0.18763	0.14862	4.63026E-05	0.189247269	0.000701884
0.01429	0.18076	0.18392	0.14042	5.73847E-05	0.20583986	0.000695099
0.01373	0.17362	0.18148	0.13479	6.81562E-05	0.219262538	0.000696921
0.01329	0.16800	0.17929	0.13118	8.07987E-05	0.232649212	0.000701581
0.01353	0.17103	0.18046	0.13294	9.44192E-05	0.245003222	0.000725321
0.01334	0.16865	0.17936	0.13176	0.000128741	0.269881119	0.000752184
0.01368	0.17302	0.18063	0.13403	0.000201225	0.3064282	0.000812784

Table 4. Experimental Results for $V_{sl}=0.0903\text{m/s}$ with Liquid Entrainment Correlations.

$V_{sl}= 0.0903\text{m/s}$						
	Rings+Liq Entrain	Probes (Bottom)	Triangular Relationship	Liquid Entrainment Correlations		
HL+Liq Entrain	Film Thickness (mm)	Film Thickness (mm)	Film Thickness	Pan & Hanratty (2002b)	Paleev & Fillippovich (1966)	Mantilla (2008)
0.02756	0.34968	0.21259	0.24284	1.05367E-05	0.120875441	0.000596097
0.02641	0.33496	0.21056	0.22368	1.30848E-05	0.136251259	0.000603718
0.02514	0.31879	0.20868	0.20703	1.7704E-05	0.157889019	0.000616625
0.02356	0.29862	0.20673	0.19245	2.44689E-05	0.181291954	0.000624689
0.02238	0.28360	0.20526	0.18504	3.07099E-05	0.197881545	0.000626701
0.02102	0.26620	0.20264	0.17463	3.76685E-05	0.212915489	0.000622168
0.01944	0.24619	0.19922	0.16446	4.71418E-05	0.229566427	0.000612997
0.01849	0.23400	0.19676	0.15629	5.72604E-05	0.24412102	0.000611549
0.01780	0.22528	0.19484	0.15165	6.8818E-05	0.257991535	0.000613694
0.01764	0.22328	0.19431	0.15162	8.12756E-05	0.270638358	0.000625869
0.01784	0.22574	0.19491	0.15210	9.66806E-05	0.283930857	0.000647159
0.01788	0.22625	0.19488	0.15145	0.000137152	0.311032887	0.00068202
0.01815	0.22975	0.19558	0.15450	0.000205867	0.343085224	0.000728772

Table 5. Experimental Results for $V_{sl}=0.1355\text{m/s}$ with Liquid Entrainment Correlations.

$V_{sl}= 0.1355\text{m/s}$						
	Rings+Liq Entrain	Probes (Bottom)	Triangular Relationship	Liquid Entrainment Correlations		
HL+Liq Entrain	Film Thickness (mm)	Film Thickness (mm)	Film Thickness	Pan & Hanratty (2002b)	Paleev & Fillippovich (1966)	Mantilla (2008)
0.03457	0.43947	0.21626	0.22367	1.01927E-05	0.195314219	0.000429514
0.03119	0.39604	0.21335	0.20353	1.50056E-05	0.221870684	0.000428117
0.03015	0.38281	0.21244	0.19722	1.95658E-05	0.240229469	0.000437098
0.02934	0.37249	0.21175	0.19142	2.64058E-05	0.26111893	0.000449972
0.02872	0.36456	0.21120	0.19045	3.13169E-05	0.273078558	0.000455276
0.02703	0.34287	0.20923	0.18198	4.05152E-05	0.291243541	0.000453727
0.02545	0.32271	0.20695	0.17506	5.03723E-05	0.306713013	0.000449773
0.02465	0.31253	0.20565	0.16948	5.93779E-05	0.318466965	0.000450753
0.02836	0.35985	0.20928	0.17279	7.74809E-05	0.337617407	0.000519825
0.02884	0.36600	0.20978	0.17678	9.11854E-05	0.349423641	0.000539053
0.02871	0.36434	0.20952	0.17548	0.0001061	0.360466299	0.000549969
0.02846	0.36115	0.20916	0.17502	0.000146966	0.384427856	0.000573253
0.02889	0.36665	0.20963	0.17732	0.000220828	0.414805523	0.000613875

Table 6. Experimental Results for $V_{sl}=0.1851\text{m/s}$ with Liquid Entrainment Correlations.

$V_{sl}=0.1851\text{m/s}$						
HL+Liq Entrain	Rings+Liq Entrain	Probes (Bottom)	Triangular Relationship	Liquid Entrainment Correlations		
	Film Thickness (mm)	Film Thickness (mm)	Film Thickness	Pan & Hanratty (2002b)	Paleev & Filippovich (1966)	Mantilla (2008)
0.04085	0.52007	0.21969	0.19066	1.09668E-05	0.26412317	0.000332846
0.03930	0.50014	0.21871	0.17970	1.55495E-05	0.287628357	0.000343469
0.03833	0.48762	0.21831	0.17710	2.09501E-05	0.307812108	0.000354511
0.03651	0.46431	0.21690	0.17153	2.73002E-05	0.325834465	0.000357693
0.03551	0.45151	0.21630	0.16777	3.4044E-05	0.340937429	0.000362948
0.03484	0.44289	0.21579	0.16848	4.25787E-05	0.356316405	0.000370816
0.03416	0.43420	0.21528	0.16794	5.40796E-05	0.372842703	0.000379482
0.03419	0.43460	0.21524	0.17067	6.80068E-05	0.388772832	0.000393733
0.03462	0.44002	0.21534	0.16986	8.08113E-05	0.400828043	0.000408152
0.03440	0.43725	0.21522	0.16813	9.66061E-05	0.413363336	0.000417459
0.03466	0.44054	0.21516	0.16832	0.000112782	0.424284989	0.000430029
0.03487	0.44321	0.21555	0.17075	0.00015998	0.449134676	0.000454396
0.03451	0.43868	0.21503	0.16743	0.000239564	0.478183455	0.000478042

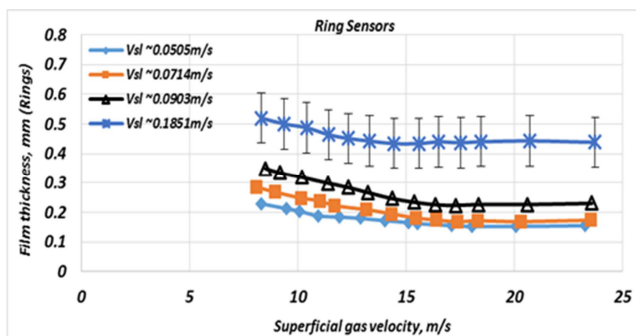
Film Thickness using Conductivity Ring Sensors.

Figure 5 is a graph of film thickness against superficial gas velocity from conductivity ring sensors. It shows that film thickness decreases with increase in superficial gas velocity as observed in Figure 4. The $V_{sl}=0.1355\text{m/s}$ had an upward projection which was because of increase in V_{sl} in the flow loop, hence was removed. The error bar plot on average $V_{sl}=0.1851\text{m/s}$ was the error propagation of $\pm 0.0844\text{mm}$ of the film thickness which shows the level of accuracy of the measured values.

Film Thickness using Triangular Relationship

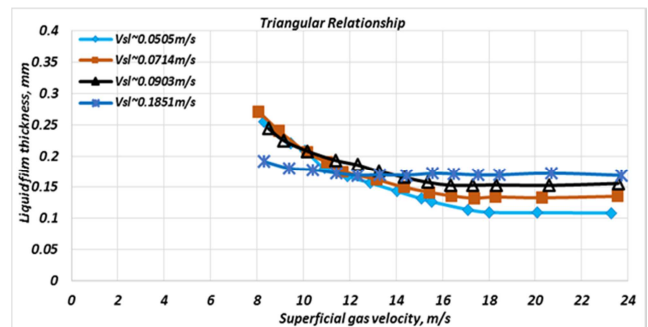
It is a unique method for determining liquid film thickness in annular flow in pipes. Triangular relationship recognizes three variables that are dependent on one another: pressure gradient, liquid film rate and liquid film thickness. It is a correlation that is based on pressure gradient and liquid film flow rate as a function of film thickness. The liquid film flow rate, could be obtained by measuring the liquid film thickness and pressure gradient on a straight pipe segment, [6, 7] clearly simplified it for flow in round tubes with assumptions that gravitational and acceleration effects are ignored. Therefore, all flow in pipes, and flows in the film including shear stress equals that of wall shear stress, other assumptions of the correlation are: all liquid flow in the pipe do not flow in the film, liquid droplets and circumferential liquid flows across pipes in annular flow. Triangular relationship for film thickness, is often used for upward flow in pipes with equation as

$$\dot{M} = f\left(\delta \frac{dp}{dz}\right) \quad (18)$$

**Figure 5.** Film thickness from ring sensor against superficial gas velocity.

From the pressure gradients and liquid flow rates from the experiments, the liquid film thickness using triangular relationship method was presented in figure 6. Figure 6, is the plot of triangular relationship (liquid film thickness) against superficial gas velocity. Triangular relationship from the graph, has shown that film thickness decreases with increase in superficial gas velocity. Again, from the same Figure 6, it was presented that the higher the superficial liquid velocity, the higher the film thickness, hence the average V_{sl} of 0.1851m/s , represented the highest film thickness in the analyses.

One observation from the graph was a uniform decline among all the superficial liquid velocity. The decline in the liquid film thickness was observed with less changes as the average superficial gas velocity increases from 16.2262m/s to 23.4575m/s . The reason is because the entrained liquid droplets overtime, will become larger due to high gas velocity that results to more break-up and lifting of these liquid droplets as superficial gas velocity increases in horizontal pipe. These liquid droplets will descend back to the bottom of the pipes through the walls of the pipes, as gravity impacts on the droplets. This phenomenon, presented the liquid film thickness plots to appear nearly as a straight line in Figure 6. The convergence on average $V_{sg}=8.2699\text{m/s}$ to 12.0675m/s in Figure 6 is because, triangular relationship presented liquid film thickness, to be decreasing with increase in superficial liquid velocity, and increasing with decrease in superficial liquid velocity. This is because triangular relationship is for annular flow in vertical pipes and not horizontal flow in pipes.

**Figure 6.** Film thickness Vs V_{sg} using Triangular Relationship.

Comparing liquid film thickness from different methods

The annular flow liquid film thickness results from the experiments, were determined using the following methods:

1. Conductivity Ring Sensors,
2. Conductance Probe Sensors and,
3. Triangular Relationship.

The results of the three methods, were plotted in Figures 7 and 8 with $V_{sl}=0.0505\text{m/s}$ and 0.0714m/s respectively, while the performance plots were presented in Figures 9 and 10, and the detailed results analysis in Tables 2-6.

The graph of Figure 7 presented a similar trend among the three methods, except the little variance from the graphs of the probes. However, conductivity ring sensors and triangular relationship plots for liquid film thickness, represents the true scenario where the liquid film thickness flows, circumferentially across entire walls of the pipes. Meanwhile, the probes only accounted for the liquid film thickness at the bottom of the pipe, hence the difference seen in Figure 7. Again, the little difference between the conductivity ring sensors and the triangular relationship could also be attributed to uncertainties from bench calibration, which was used in determining film thickness for the conductivity ring sensors' method.

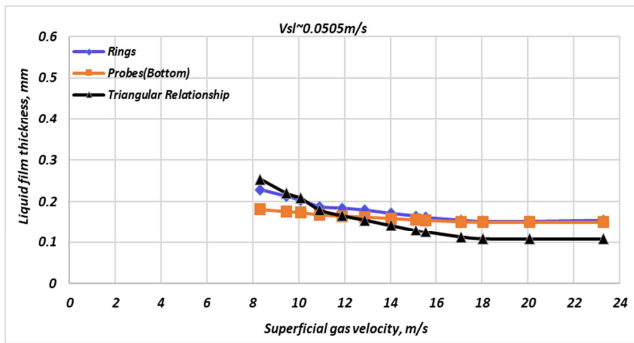


Figure 7. Comparing film thickness from three methods ($V_{sl} \sim 0.0505\text{m/s}$).

From figure 8, the film thickness from conductivity rings sensors and the triangular relationship showed similar trend while the plot from probes was a bit different from that of average superficial gas velocities of 8.2699m/s to 14.2883m/s . Again, the probe represents, only the film thickness at the bottom of the pipe which is the difference in the plots.

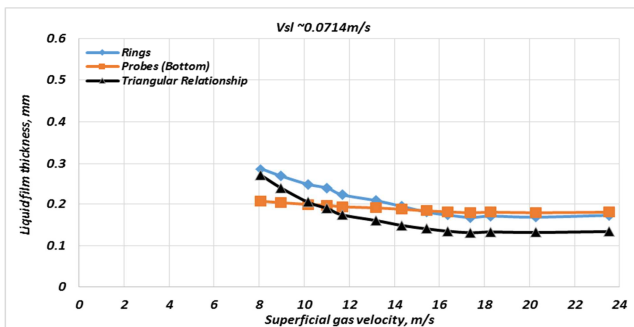


Figure 8. Comparing film thickness from three methods ($V_{sl} \sim 0.0714\text{m/s}$).

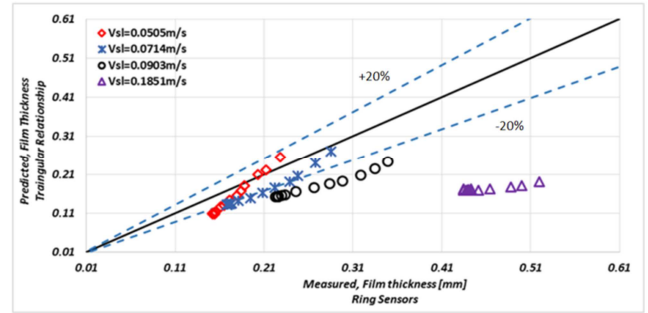


Figure 9. Plot of Predicted against Measured Liquid Film Thickness from Ring Sensors.

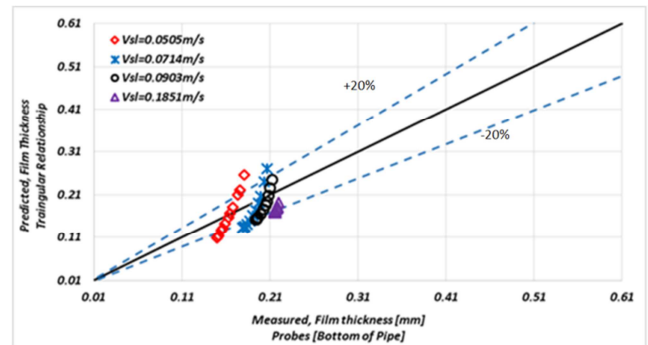


Figure 10. Plot of Predicted against Measured Liquid Film Thickness from Probes.

The graphs of Figures 9 and 10 are the predicted liquid film thickness from triangular relationship against the measured film thickness from conductivity ring sensors and probes. From Figure 9, the liquid film thickness from triangular relationship under-predicted liquid film thickness, when compared with liquid film thickness from conductivity ring sensors. The plot of average $V_{sl}=0.1851\text{m/s}$ was completely off, showing a wide difference while plots of $V_{sl}=0.0505\text{m/s}$ and $V_{sl}=0.0714\text{m/s}$, preferably matched. For probes, the predicted triangular relationship liquid film thickness matched better with the measured liquid film thickness from probes in all the superficial liquid velocities. This is to illustrate that probes detects liquid film thickness better than conductivity ring sensors in annular flow as seen Figure 8. The reason is because of the impact of high superficial gas velocity on conductivity ring sensors which will be a green area for future research in annular flow in pipes.

4. Conclusion

To understand the dynamics of annular flow in pipes, liquid film thickness was analyzed. Liquid film thickness in all the flow matrix in this study were observed decreasing with increase in gas velocity while increasing with increase in liquid velocity. The decreasing tendency with gas velocity was because of liquid entrainment. The liquid entrainments, were accounted for using [17] correlation. The correlation gave the more realistic results among other correlations compared from the experimental data. This was further proven by [10] analysis on liquid entrainment correlations for horizontal pipes where [17] was presented as a correlation

that preferably, predicts liquid entrainment.

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