
Quiver of hyperstructures for Ying's twin universes

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Abstract: The quiver of hyperstructures, especially very large classes of them, can be used in new scientific theories such as Ying's twin universes. We present the largest class of hyperstructures which can be used as a model to represent the twin universe cosmos as even more new axioms or conditions are considered.

Keywords: Hyperstructure, H_v -Structure, Hope, Twin Universe

1. Introduction

Traveling in hyperstructures and their representations one can see some very beautiful landscape and fascinating site-views: H_v -groups, H_v -rings, H_v -fields, H_v -vector spaces, H_v -Lie algebras. We have to transfer as many possible results from classical theories, and since hyperstructure theory is very large, especially the weak ones, the problem becomes difficult but aesthetically beautiful. Weak axioms give larger classes and their associated applications. As new axioms appeared, new terms and constructions are introduced in order to manipulate and to classify the large classes of new hyperstructures.

The new theories in sciences, especially the revolutionary ones, need a very large class of structures in order that the researcher can select the most appropriate to express the theoretical background to improve the results. In this note I will present H_v -structures which can be used in the Ying's twin universe theories [1, 2, 3] composed of two anti-symmetric systems which have two universes of 4-dimensional space-time coexisting on opposite sides of a 2-dimensional membrane.

2. Basic Definitions

Hyperstructures are called algebraic structures equipped with at least one hyperoperation (abbreviated to *hope*) [4]. *Weak hyperstructures* introduced in 1990 [5] are called H_v -structures and are defined as follows:

In a set H equipped with a hope $\cdot: H \times H \rightarrow \mathcal{P}(H)$, we abbreviate by *WASS* the weak associativity: $(xy)z \cap x(yz) \neq \emptyset, \forall x, y, z \in H$ and by *COW* the weak

commutativity: $xy \cap yx \neq \emptyset, \forall x, y \in H$.

The hyperstructure (H, \cdot) is called H_v -semigroup if it is *WASS*, is called H_v -group if it is reproductive H_v -semigroup: $xH = Hx = H, \forall x \in H$. $(R, +, \cdot)$ is called H_v -ring if $(+)$ and (\cdot) are *WASS*, the reproduction axiom is valid for $(+)$ and (\cdot) is *weak distributive* with respect to $(+)$:

$$x(y + z) \cap (xy + xz) \neq \emptyset, (x + y)z \cap (xz + yz) \neq \emptyset, \\ \forall x, y, z \in R$$

For more definitions, results and applications on H_v -structures, see [6, 7, 8, 9, 10]. An extreme class is the following: an H_v -structure is *very thin* if all hopes are operations except one, with all hyperproducts singletons except only one, which is a subset with cardinality more than one.

The *fundamental relations* β^* and γ^* are defined, in H_v -groups and H_v -rings, respectively, as the smallest equivalences so that the quotient would be group and ring, respectively.

Theorem 2.1 Let (H, \cdot) be H_v -group and let us denote by U the set of all finite products of elements of H . We define the relation β in H as follows: $x\beta y$ if $\{x, y\} \subset u$ where $u \in U$. Then the fundamental relation β^* is the transitive closure of the relation β .

An element is called *single* if its fundamental class is a singleton.

Motivation for H_v -structures:

(A) The quotient of a group with respect to an invariant subgroup is a group.

(B) F. Marty states that, the quotient of a group by any subgroup is a hypergroup.

(C) Now, the quotient of a group with respect to any partition is an H_V -group.

Definition 2.2 Let (H, \cdot) , (H, \otimes) be H_V -semigroups defined on the same H . (\cdot) is smaller than (\otimes) , and (\otimes) greater than (\cdot) , if there exists automorphism $f \in \text{Aut}(H, \otimes)$ such that $xy \subset f(x \otimes y)$, $\forall x, y \in H$. Then (H, \otimes) contains (H, \cdot) and write $\cdot \leq \otimes$. If (H, \cdot) is a structure, then it is basic and (H, \otimes) is an H_b -structure.

The Little Theorem. Greater hopes of the ones which are *WASS* or *COW*, are also *WASS* and *COW*, respectively.

Definition 2.3 [5, 6] The H_V -ring $(R, +, \cdot)$ is an H_V -field if the quotient R/γ^* is a field.

Definitions 2.4 [6] Let $(F, +, \cdot)$ be an H_V -field, $(V, +)$ be *COW* H_V -group and there exists an external hope $\cdot: F \times V \rightarrow P(V)$: $(a, x) \rightarrow ax$ such that, $\forall a, b \in F, \forall x, y \in V$ we have

$$a(x+y) \cap (ax+ay) \neq \emptyset, (a+b)x \cap (ax+bx) \neq \emptyset, (ab)x \cap a(bx) \neq \emptyset,$$

then V is called an H_V -vector space over F .

In the above cases the fundamental relation ε^* is defined to be the smallest equivalence relation such that the quotient V/ε^* is a vector space over the field F/γ^* .

The general definition of an H_V -Lie algebra was given in [11] as follows:

Definition 2.5 Let $(L, +)$ be H_V -vector space over the field $(F, +, \cdot)$, $\phi: F \rightarrow F/\gamma^*$, the canonical map and $\omega_F = \{x \in F: \phi(x) = 0\}$, where 0 is the zero of the fundamental field F/γ^* . Similarly, let ω_L be the core of the canonical map $\phi': L \rightarrow L/\varepsilon^*$ and denote by the same symbol 0 the zero of L/ε^* . Consider the bracket (commutator) hope:

$$[\cdot, \cdot]: L \times L \rightarrow P(L): (x, y) \rightarrow [x, y]$$

then L is an H_V -Lie algebra over F if the following axioms are satisfied:

(L1) The bracket hope is bilinear, i.e.

$$[\lambda_1 x_1 + \lambda_2 x_2, y] \cap (\lambda_1 [x_1, y] + \lambda_2 [x_2, y]) \neq \emptyset$$

$$[x, \lambda_1 y_1 + \lambda_2 y_2] \cap (\lambda_1 [x, y_1] + \lambda_2 [x, y_2]) \neq \emptyset,$$

$$\forall x, x_1, x_2, y, y_1, y_2 \in L \text{ and } \lambda_1, \lambda_2 \in F$$

(L2) $[x, x] \cap \omega_L \neq \emptyset, \forall x \in L$

(L3) $([x, [y, z]] + [y, [z, x]] + [z, [x, y]]) \cap \omega_L \neq \emptyset, \forall x, y \in L$

3. Classes of H_V -Structures

Definition 3.1 [6]. Let (G, \cdot) be groupoid, then for all P such that $\emptyset \neq P \subset G$, define the following hopes called *P-hopes*: $\forall x, y \in G$

$$P: xPy = (xP)y \cup x(Py), P_r: xP_r y = (xy)P \cup x(Py),$$

$$P_l: xP_l y = (Px)y \cup P(xy).$$

The (G, P) , (G, P_r) , (G, P_l) are called *P-hyperstructures*. The most usual case is if (G, \cdot) is semigroup, then $xPy = (xP)y \cup x(Py) = xPy$, and (G, P) is a semihypergroup.

Definitions 3.2 [8]. Let (G, \cdot) be groupoid (resp.,

hypergroupoid) and $f: G \rightarrow G$ be a map. We define a hope (∂) , called *theta-hope* or simply *∂-hope*, on G as follows

$$x\partial y = \{f(x) \cdot y, x \cdot f(y)\}, \forall x, y \in G. \text{ (resp. } x\partial y = (f(x) \cdot y) \cup (x \cdot f(y)), \forall x, y \in G)$$

If (\cdot) is commutative then (∂) is commutative. If (\cdot) is *COW*, then (∂) is *COW*.

Let (G, \cdot) be groupoid (resp. hypergroupoid) and $f: G \rightarrow P(G) - \{\emptyset\}$ be multivalued map. We define ∂ , on G as follows

$$x\partial y = (f(x) \cdot y) \cup (x \cdot f(y)), \forall x, y \in G.$$

Basic Property. If (G, \cdot) is a semigroup then, for every f , the (∂) is *WASS*.

Let (G, \cdot) be a groupoid and $f_i: G \rightarrow G, i \in I$, be a set of maps on G . We consider the map $f_\cup: G \rightarrow P(G)$ such that $f_\cup(x) = \{f_i(x) \mid i \in I\}$, called the union of the $f_i(x)$. We define the union ∂ -hope, on G if we consider as map the $f_\cup(x)$. A special case for a given map f , is to take the union of this with the identity map. We consider the map $f \equiv f \cup (\text{id})$, so $f(x) = \{x, f(x)\}, \forall x \in G$, which we call *b-∂-hope*. Then we have:

$$x\partial y = \{xy, f(x) \cdot y, x \cdot f(y)\}, \forall x, y \in G.$$

In weak hyperstructures we can enlarge or reduce the underline set so that we can have H_V -structures with more properties [9]. Enlargements or reductions are more useful in representation theory if the obtain H_V -structures have the same fundamental structure.

Construction 3.3 The Attach Construction. Let (H, \cdot) be an H_V -semigroup and $v \notin H$. We extend the (\cdot) into the set $H = H \cup \{v\}$ as follows:

$$x \cdot v = v \cdot x = v, \forall x \in H, \text{ and } v \cdot v = H.$$

The (H, \cdot) is an *h/v-group*, i.e. there is a reproductivity on classes, where $(H, \cdot) / \beta^* \cong Z_2$ and v is a single element.

The hyperstructure (H, \cdot) is called *attach h/v-group* of (H, \cdot) .

Remarks. The core of (H, \cdot) is the set H . All scalar elements of (H, \cdot) are also scalars in (H, \cdot) and any unit element of (H, \cdot) is also a unit of (H, \cdot) . Finally, if (H, \cdot) is *COW* (resp. commutative) then (H, \cdot) is also *COW* (resp. commutative).

Definitions 3.4 Let (H, \cdot) be a hypergroupoid.

We say that we *remove* $h \in H$, if we simply consider the restriction of (\cdot) on $H - \{h\}$.

We say that $h \in H$ *absorbs* $h \in H$ if we replace h , whenever it appears, by h .

We say that $h \in H$ *merges* with $h \in H$, if we take as product of $x \in H$ by h , the union of the results of x with both h and h , and consider h and h as one class, with representative h .

4. H_V -Structures Defined on Small Sets

To compare classes we can see on the problem of enumeration and classification of H_V -structures on the small sets. Recently we have interesting results by using computers.

The problem is complicate in H_v -structures because we have great numbers. The partial order introduced in H_v -structures, restrict the problem in finding the minimal, *up to isomorphisms*, H_v -structures. In this direction we have results by Bayon & Lygeros as the following [12]:

The number of H_v -groups with three elements is 1.026.462. The 7.926 are abelians and the rest are not; 1.013.598 are cyclic and 12.864 are not, 16 are very thin.

Up to isomorphism, in sets with three elements there are: 6.494 minimal H_v -groups. 137 are abelians and the rest are not;

From the H_v -groups with 4 elements: the 8.028.299.905 are abelian H_v -groups, from which the 7.995.884.377 are cyclic.

In order to compare the numbers we see that: There are 10.614.362 classical abelian hypergroups, from which the 10.607.666 are cyclic.

From the above it is clear that the number of the H_v -structures is enormous comparing to the classical hyperstructures.

5. Applications

A new application of the hyperstructure theory in social sciences combining the hyperstructure and fuzzy theory, is to replace in questionnaires the scale of Likert by the bar of Vougiouklis & Vougiouklis [13]. The hyperstructures are used as an organized device. The suggestion is the following: In every question substitute the Likert scale with 'the *bar*' whose poles are defined with '0' on the left end, and '1' on the right end:

$$0 \text{ ————— } 1$$

The subjects/participants are asked instead of deciding and checking a specific grade on the scale, to cut the bar at any point they feel expresses their answer to the specific question. The use of the bar of Vougiouklis & Vougiouklis instead of a scale of Likert has several advantages during both the filling-in and the research processing. The length of the bar is according to the Golden Ratio 6.2cm. The hyperstructure theory, gives innovating new suggestions to connect finite groups of objects. These suggestions are obtained from properties and special elements inside the hyperstructure.

The Lie-Santilli *isotopies* born to solve Hadronic Mechanics problems. Santilli proposed [14, 15] a 'lifting' of the trivial unit matrix of a normal theory into a nowhere singular, symmetric, real-valued, new matrix. The original theory is reconstructed such as to admit the new matrix as left and right unit. The *isofields* needed correspond to H_v -structures called *e-hyperfields* which are used in physics or biology. *Definition:* Let $(H_o, +, \cdot)$ be the attached H_v -field of the H_v -semigroup (H, \cdot) . If (H, \cdot) has a left and right scalar unit e then $(H_o, +, \cdot)$ is *e-hyperfield*, the *attached H_v -field of (H, \cdot)* .

In [14] a *P-hope* was introduces which is appropriate for *e-hyperstructures*:

Construction 5.1 Let (G, \cdot) be abelian group and P any subset of G with more than one elements. We define the hyperoperation \times_P as follows:

$$x \times_P y = \begin{cases} x \cdot P \cdot y = \{x \cdot h \cdot y \mid h \in P\} & \text{if } x \neq e \text{ and } y \neq e \\ x \cdot y & \text{if } x = e \text{ or } y = e \end{cases}$$

we call this hope *P_e-hope*. The hyperstructure (G, \times_P) is an abelian H_v -group.

6. Ying's Twin Universe

The new theories in sciences, especially the revolutionary ones, need a very large class of structures in order that the researcher could select the most appropriate to express the theoretical background and to improve the results. Therefore, from paragraph 4, it is clear that one can select the appropriate model from the huge number of the offered H_v -structures.

The Ying's Twin Universe [1, 2, 3] is the Total Universe which is composed of two anti-symmetric systems which have two universes of 4-dimensional space-time coexisting on opposite sides of a 2-dimensional membrane. That means than it has a Positive Universe and a Negative Universe and together with the membrane gives a total of 10-dimensions 'Cosmos'. Consequently, in the model we suggest to use:

1. An appropriate hyperfield from the class of H_v -fields to take the hypernumbers.
2. Two weak homomorphic 4-dimensional hyper- (H_v) -space-time coexisting on opposite sides over the above H_v -fields.
3. A 2-dimensional hyper- (H_v) -space.
4. Weak homomorphisms to transfer properties from one H_v -space-time to the other especially on the fundamental classes.

All the above generalizations must have as a special case the single value representation on the corresponding fundamental structures. Adding new axioms and conditions will restrict the cases of H_v -fields.

We suppose that we must have two weak homomorphic 4-dimensional hyper (H_v) spacetime coexisting in order the model to admit some different cases on the opposite sides. This means that we can have even different axioms provided only that on the fundamental classes we have an ordinary Universe. In other words, we can partition on the Universes so that to have homomorphic models. To simplify the model we can use only one H_v -field, with fundamental field the complex field and to take the Cartesian product or the Cayleyen construction.

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