

Communication

Application of Taguchi Method for Optimum Weld Process Parameters of Pure Aluminum

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Abstract: Though many optimization methods have been developed, there is a lack of comparative study regarding the performance of those methods. This paper demonstrates the adequacy as well as the simplicity of the Taguchi method on the selection of optimum process parameters of the MIG welding as well as the TIG welding of pure aluminum by comparing the grey rational analysis results of Joshi and his co-workers. ANOVA results are utilized to identify the optimum weld process parameters (viz. welding current, gas flow and wire feed rate) and estimated the possible optimum ultimate tensile strength of the aluminum weld joint, by means of additive law. The estimates are found to be reasonably in good agreement with test results, when compared to those from the empirical relations of Joshi and his co-workers.

Keywords: ANOVA, MIG Welding, Aluminum, Tensile Strength, TIG Welding

1. Introduction

Pure aluminum having poor strength is improved by alloying with other metals. Light weight materials like aluminum alloys possessing high specific strength and corrosion resistance are being used in automotive and aerospace industries. Many components are made by casting and few of them may require welding. They will be loaded statically and dynamically as per requirement. Metal inert gas (MIG) welding and tungsten inert gas (TIG) welding (see Figure 1) are widely used techniques for joining ferrous and non-ferrous metals. Both welding processes initially superheat the parent metals into a liquid state, and finally a filler material is used to fuse the parent metals together. They use a shielding during welding process. MIG welding runs the filler material from a wire coil through the MIG torch. This wire carries the electrical current, and does the actual welding. TIG welding uses a tungsten electrode to superheat the parent metals. The filler material will be dabbed onto the weld puddle. The sharpened tungsten electrode is poking out

the front of the torch when the two metals have reached a liquid state. TIG welding uses pure argon welding gas, whereas MIG welding generally uses a mix of 25% Argon, 75% CO₂. TIG welding process is a more versatile than the MIG welding process due to quick changing of the filler material by just grabbing another rod, whereas MIG welding requires a wire change.

In general, the quality of a weld joint is influenced by the weld input process parameters. This is the reason why the welding is considered as a multi-input and multi-output process. Hence there is a necessity for identifying the optimum weld process parameters to achieve the required quality of a weld joint with minimal detrimental residual stresses and distortion. Various optimization techniques have been adopted to specify the optimum weld process parameters for achieving the required quality of a weld joint, and to avoid the time-consuming trial and error developmental efforts of the process engineers.

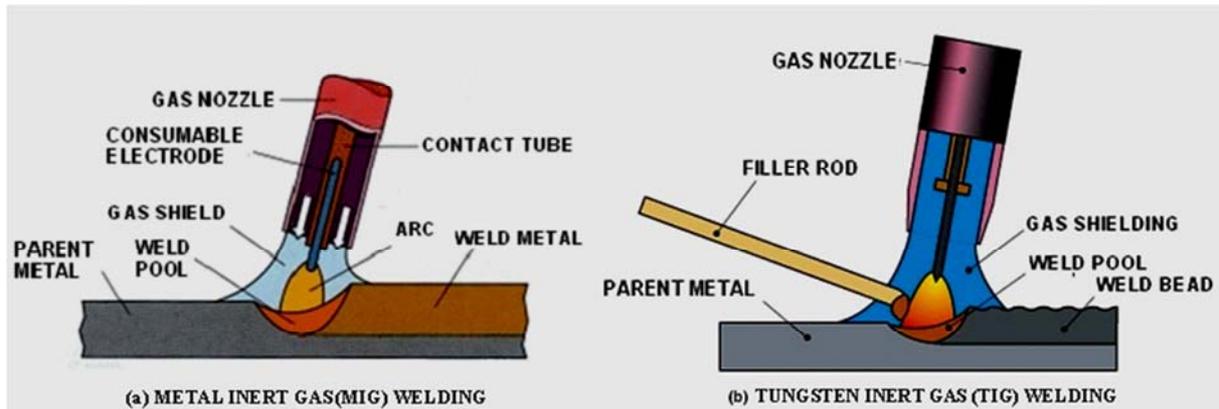


Figure 1. Inert gas welding.

Saluja and Moeed [1] have adopted the factorial design approach to examine the MIG welding parameters (*viz.*, welding current, arc voltage, stick-out distance of electrode and welding speed) on aluminum by measuring bead geometry and weld penetration. They have developed a mathematical model for sound quality bead width, bead penetration and weld reinforcement on butt joint. The welding current is found to be the most influencing parameter on the weld geometry. Patel and Gandhi [2] have recorded tensile strength for MIG welding parameters such as welding current, welding speed, flow of shielding gas and arc voltage. It is noted that the tensile strength increases with increasing the welding current. Palani and Saju [3] have examined the TIG welding process parameters (*viz.*, welding speed, current and gas flow rate) on welding of aluminium and used the response surface methodology to conduct the experiments for measuring the strength of weld joints. It is noted that welding current is highly influencing parameter on the tensile strength and percent elongation. Haragopal and Ravindra Reddy [4] have applied Taguchi method to study the effect of gas pressure, current, groove angle and preheat on MIG welding of Al- 65032. Welding current is found to influence the ultimate tensile strength. Gas pressure is found to be the significant parameter for proof stress, elongation and impact energy. Padmanaban and Balasubramanian [5] have studied the effect of pulsed current gas tungsten arc welding process parameters on tensile strength in AZ31B magnesium alloy. The pulse frequency has the greatest influence on tensile strength, followed by peak current, pulse on-time and base current.

Joshi *et al.* [6] have adopted the full factorial method in their experimental design to generate the tensile strength values for all combination levels of the welding parameters (*viz.*, welding current, gas flow and wire feed rate for MIG welding, whereas welding current and gas flow for TIG welding). The grey relational analysis (GRA) technique has been used to perform parametric optimization. The method of approach followed by Joshi *et al.* [6] requires more number of experiments. It is preferable to have less number of experiments by adopting the Taguchi's approach, which uses the orthogonal array to study large number of design

variables by conducting minimum number of experiments. Saxena *et al.* [7] have examined the influence of MIG welding parameters on tensile strength of AM-40 (EN AW5083) aluminum alloy using Taguchi technique. Welding current and welding voltage are influencing the tensile strength of welded joint. The signal-to-noise (S/N) ratio transformation in the Taguchi's design of experiments considered by Saxena *et al.* [7] is on a single value of each test run output response. In fact, Taguchi has created the S/N ratio transformation to consolidate several repetitions into one value to reflect the amount of variation present. Hence, the unwanted S/N ratio transformation adopted by them has no added advantage other than additional computational work. Flux bounded tungsten inert gas welding process is recommended to improve penetration capability of TIG process for joining of aluminum alloys [8-10]. Several optimization methods have been adopted for modeling, control and optimizing the different weld process to achieve a good quality of weld joints [11-18]. There is a lack of comparative study regarding the performance of those methods.

This paper examines the adequacy of the Taguchi method on the selection of optimum process parameters of the MIG welding as well as the TIG welding of pure aluminum by comparing the grey rational analysis results of Joshi and his co-workers [6]. ANOVA results are utilized to identify the optimum weld process parameters (*viz.* welding current, gas flow and wire feed rate). The optimum ultimate tensile strength of the aluminum weld joint is estimated by means of additive law. The estimates are found to be reasonably in good agreement with test results, when compared to those obtained from the empirical relations of Joshi and his co-workers [6]. This study clearly demonstrates the simplicity of the Taguchi method to obtain optimum weld process parameters to achieve maximum ultimate tensile strength of pure aluminum through less number of experiments. In order to improve the estimates of the UTS for MIG and TIG weld joints, fictitious input parameters are introduced without changing the test runs. Test results are found to be within the expected range of the UTS values for both MIG and TIG weld joints.

2. Taguchi's Design of Experiments and Analysis of Variance

The work-piece is made of pure aluminum (>99.5% Al) of 1xxx series, which is a soft material having low mechanical strength and high conductivity. It has 10mm thickness, 50.8mm width and 125mm length. It is a butt joint with complete penetration groove. The design of experiments involves selection of independent variables or factors (viz., electric current, feed rate and gas flow); selection of number of level setting for each independent variable; selection of orthogonal array; assignment of independent variable to each column of orthogonal array; conducting experiments for measuring the ultimate tensile strength of the butt joint. Table-1 gives the assignment levels of process parameters [6] and the performance output response (viz., the ultimate tensile strength) for the assigned process parameters as per L₉ orthogonal array. Analysis of variance (ANOVA) is performed as in Refs.19 and 20 to trace the optimum process parameters for obtaining maximum ultimate tensile strength (UTS) of the weld joint. It is noted from the ANOVA results of Table-2 that electric current, feed rate and gas flow effect on the UTS are 36.8, 30.3 and 32.9% respectively.

Table 1. Performance output response, viz., the ultimate tensile strength (UTS) of the weld joint for the assigned process parameters as per L₉ orthogonal array (MIG welding).

Assignment levels of process parameters in MIG welding.

Control Factors (Input parameters)	Designate d Factor	Level -1	Level-2	Level -3
Electric current (Amp)	A	135	145	155
Feed rate (ft/min)	B	9	10	11
Gas flow (lit/min)	C	15	20	25

Performance output response, viz., the ultimate tensile strength (UTS).

Test Run	Levels of input parameters			UTS (MPa)		
	A	B	C	Test [6]	Eq.(1)	Eq.(2) [6]
1	1	1	1	69.21	68.00	69.29
2	1	2	2	75.46	77.06	73.56
3	1	3	3	78.63	77.31	77.84
4	2	1	2	74.53	73.22	75.60
5	2	2	3	78.12	76.90	79.95
6	2	3	1	70.17	72.72	75.41
7	3	1	3	75.04	77.60	81.92
8	3	2	1	79.12	77.81	77.45
9	3	3	2	84.67	83.45	81.72

Table 2. Analysis of variance (ANOVA) for the UTS (MPa) of the weld joint in MIG welding.

Parameters	1-Mean	2-Mean	3-Mean	Sum of squares	% contribution
A	74.43	74.27	79.61	55.30	36.8
B	72.93	77.57	77.82	45.57	30.3
C	72.83	78.22	77.26	49.56	32.9

The process parameters for the maximum UTS

corresponding to MIG welding are A₃ B₃ C₂. Here subscripts denote the level of the parameter. Conformation experiments are necessary to find the output responses for the identified optimum process parameters. However, there is a possibility of estimating the optimal output response for the desired process parameters by means of additive law [21]:

$$\hat{\eta} = \eta_m + \sum_{i=1}^p (\eta_i - \eta_m) \tag{1}$$

Here $\hat{\eta}$ is the optimum value for the output response; η_m is the overall mean of η with 9 test runs; η_i is the mean of η at the optimal level for the process parameters (i); and p is the number of process parameters. The empirical relation for ultimate tensile strength (UTS) developed by Joshi et al. [6] for MIG welding is

$$UTS = 2.4 + 0.340 \times A + 1.36 \times B + 0.583 \times C \tag{2}$$

The estimated value of the UTS corresponding to the MIG welding is 83.44 MPa, which is found to be in good agreement with the test result of 84.67 MPa in Table1. The mathematical model of Ref.6 given in equation (2) provides the UTS value for the optimum process parameters as 81.72 MPa. Equation (1) can be used for estimation of the output response (in the present study, the UTS) for each test run by considering η_i as the mean value of η at the level of the process parameter (i). It should be noted that the estimates of the UTS of MIG welding for each test run using equation (1) in Table 1 are reasonably in good agreement with test results as well as those obtained from the empirical relation (2) of Joshi et al. [6]. Figure 2 shows the comparison of experimental and estimated output response, viz., the ultimate tensile strength (UTS) in MIG welding for all possible levels of the input variables. The estimated values of the UTS are found to be in reasonably good agreement with test results as well as the mathematical model [6]. The discrepancy in predictions is mainly due to scatter in the test results of UTS.

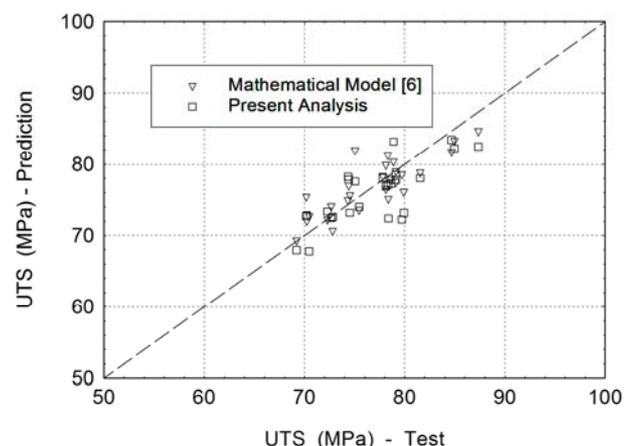


Figure 2. Comparison of experimental and estimated ultimate tensile strength (UTS) in MIG welding.

Table 3. Performance output response, viz., the ultimate tensile strength (UTS) of the weld joint for the assigned process parameters as per L_9 orthogonal array (TIG welding).

Assignment levels of process parameters in TIG welding.

Control Factors (Input parameters)	Designated Factor	Level -1	Level-2	Level-3
Electric current (Am)	A	210	225	240
Gas flow (lit/min)	C	6	7	8

Performance output response, viz., the ultimate tensile strength (UTS).

Test Run	Levels of input parameters		UTS (MPa)		
	A	C	Test [6]	Eq.(1)	Eq.(3) [6]
1	1	1	64.29	66.93	69.08
2	1	2	60.19	62.15	68.20
3	1	3	69.74	65.16	67.32
4	2	1	87.48	84.12	75.62
5	2	2	79.79	79.34	74.74
6	2	3	78.53	82.35	73.86
7	3	1	79.28	80.02	82.16
8	3	2	76.73	75.24	81.28
9	3	3	77.48	78.25	80.40

Table 3 gives the assignment levels of process parameters in TIG welding [6] and the performance of output response (viz., the ultimate tensile strength) for the assigned process parameters as per L_9 orthogonal array. Analysis of variance (ANOVA) is performed as in Refs.19 and 20 to trace the optimum process parameters for obtaining maximum ultimate tensile strength (UTS) of the weld joint. It is noted from the ANOVA results of Table 4 that electric current and gas flow effect on the UTS in TIG welding are 93.2 and 6.8% respectively. The process parameters for the maximum UTS corresponding to TIG welding are found to be $A_2 C_1$. The estimated value of the UTS corresponding to the TIG

welding is 84.12 MPa, which is found to be in good agreement with the test result of 87.48 MPa in Table 3.

Table 4. Analysis of variance (ANOVA) for the UTS (MPa) of the weld joint in TIG welding.

Parameters	1-Mean	2-Mean	3-Mean	Sum of squares	% contribution
A	64.74	81.93	77.83	483.79	93.2
C	77.02	72.24	75.25	35.05	6.8

The empirical relation for ultimate tensile strength (UTS) developed by Joshi et al. [6] for TIG welding is

$$UTS = -17.2 + 0.436 \times A - 0.88 \times C \quad (3)$$

The mathematical model of Ref.6 given in equation (3) provides the UTS value in TIG welding for the optimum process parameters as 75.62 MPa. Equation (1) is used for estimation of UTS for each test run by considering η_i as the mean value of η at the level of the process parameter (i). The estimates of the UTS of MIG welding for each test run using equation (1) in Table-3 are reasonably in good agreement with test results as well as those obtained from the empirical relation (3) of Joshi et al. [6]. Figure 3 shows the comparison of experimental and estimated output response, viz., the ultimate tensile strength (UTS) in TIG welding for all possible levels of the input variables. The estimated values of the UTS are found to be in reasonably good agreement with test results as well as the mathematical model [6]. The discrepancy in predictions is mainly due to scatter in the test results of UTS.

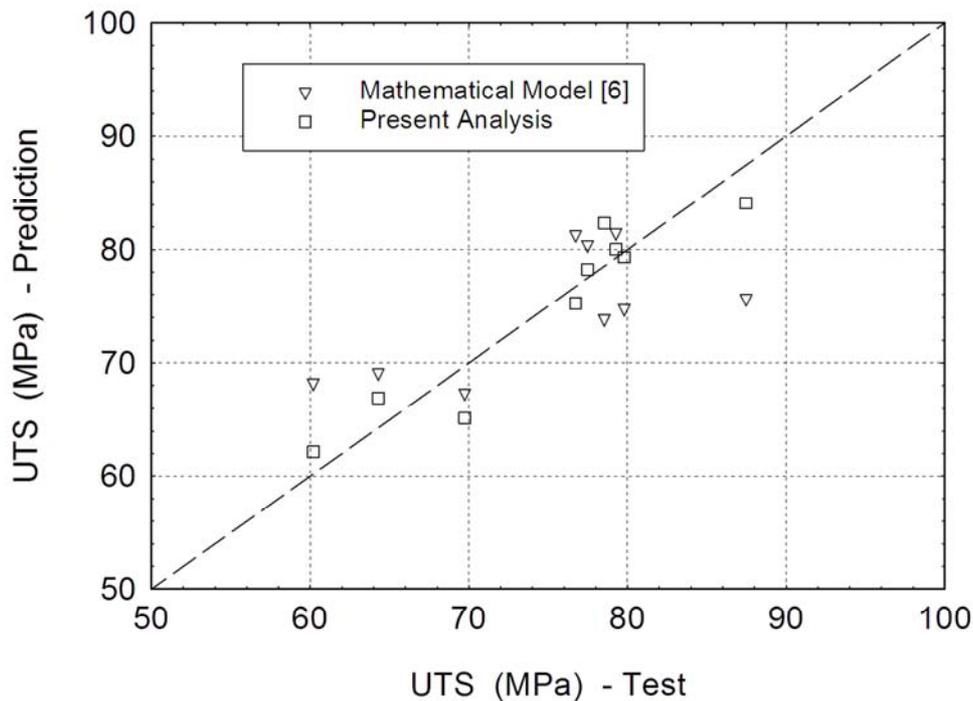


Figure 3. Comparison of experimental and estimated ultimate tensile strength (UTS) in TIG welding.

An attempt is made to improve the estimations by introducing fictitious input parameters for the same test runs. As per the Taguchi design of experiments, the relation between the number of experiments ($N_{Taguchi}$), and the factors or input parameters with their assigned levels is

$$N_{Taguchi} = 1 + \text{Number of factors} \times (\text{Number of Levels} - 1) \quad (4)$$

When $N_{Taguchi} = 9$ and $\text{Number of Levels} = 3$, equation (4) gives 4 number of factors that can be accommodated. In MIG welding the number of factors considered in Ref.6 is 3, whereas it is 2 for TIG welding. A fictitious factor F is introduced for MIG welding and two fictitious factors F1 and F2 for TIG welding. ANOVA has been performed for both MIG and TIG welding processes and estimated the UTS for the assigned levels. Equation (1) is used for estimation of UTS for each test run by considering η_i as the mean value of η at the level of the process parameter (i). In case of fictitious parameters, the levels of lowest and highest mean values of η are considered to specify the expected range of the UTS. The estimates of UTS in Tables 5 and 6 are found to be close to the test results. Most of the results are found to be within the expected range of UTS.

Table 5. Performance output response, viz., the ultimate tensile strength (UTS) of the weld joint for the assigned process parameters as per L_9 orthogonal array (MIG welding).

Assignment levels of process parameters.

Control Factors (Input parameters)	Designated Factor	Level -1	Level-2	Level-3
Electric current (Amp)	A	135	145	155
Feed rate (ft/min)	B	9	10	11
Gas flow (lit/min)	C	15	20	25
Fictitious	F	f_1	f_2	f_3

Performance output response, viz., the ultimate tensile strength (UTS).

Test Run	Levels of input parameters				UTS (MPa)		
	A	B	C	F	Test [6]	Eq.(1)	Expected Range
1	1	1	1	1	69.21	69.23	65.46 – 69.33
2	1	2	2	2	75.46	74.52	74.52 – 78.39
3	1	3	3	3	78.63	78.64	74.77 – 78.64
4	2	1	2	3	74.53	74.55	70.68 – 74.55
5	2	2	3	1	78.12	78.13	74.36 – 78.23
6	2	3	1	2	70.17	70.18	70.18 – 74.05
7	3	1	3	2	75.04	75.06	75.06 – 78.93
8	3	2	1	3	79.12	79.13	75.27 – 79.14
9	3	3	2	1	84.67	84.68	80.91 – 84.78

Analysis of variance (ANOVA) on the UTS (MPa).

Parameters	1-Mean	2-Mean	3-Mean	Sum of squares	% contribution
A	74.43	74.27	79.61	55.30	30.8
B	72.93	77.57	77.82	45.57	25.4
C	72.83	78.22	77.26	49.56	27.6
F	77.33	73.56	77.43	29.20	16.2

Table 6. Performance output response, viz., the ultimate tensile strength (UTS) of the weld joint for the assigned process parameters as per L_9 orthogonal array (TIG welding).

Assignment levels of process parameters.

Control Factors (Input parameters)	Designated Factor	Level -1	Level-2	Level-3
Electric current (Am)	A	210	225	240
Gas flow (lit/min)	C	6	7	8
Fictitious	F1	f_1	f_2	f_3
Fictitious	F2	f_4	f_5	f_6

Performance output response, viz., the ultimate tensile strength (UTS).

Test Run	Levels of input parameters				UTS (MPa)		
	A	C	F1	F2	Test [6]	Eq.(1)	Expected Range
1	1	1	1	1	64.29	65.15	63.97 – 71.52
2	1	2	2	2	60.19	60.21	59.19 – 66.74
3	1	3	3	3	69.74	69.75	62.20 – 69.75
4	2	1	2	3	87.48	87.49	81.16 – 88.71
5	2	2	3	1	79.79	79.80	76.38 – 83.93
6	2	3	1	2	78.53	79.39	79.39 – 86.95
7	3	1	3	2	79.28	79.30	77.06 – 84.61
8	3	2	1	3	76.73	77.59	72.28 – 79.83
9	3	3	2	1	77.48	77.67	75.29 – 82.84

Analysis of variance (ANOVA) on the UTS (MPa).

Parameters	1-Mean	2-Mean	3-Mean	Sum of squares	% contribution
A	64.74	81.93	77.83	483.79	84.3
C	77.02	72.24	75.25	35.05	6.1
F1	74.03	75.05	76.27	8.28	1.4
F2	73.85	72.67	77.98	46.65	8.2

3. Conclusion

Studies are made in this paper to examine the influence of weld parameters (viz., electric current, feed rate and gas flow) on MIG welding and TIG welding process. Based on the Taguchi's design of experiments and ANOVA analysis, the percentage contribution of MIG welding for welding current is 36.8%, gas flow of 32.9% and feed rate of 30.3%. The percentage contribution of TIG welding for welding current is 93.2% and gas flow of 6.8%. The electric current is considered as the most significant parameter for both MIG and TIG welding. The optimal parameter combination is meeting at experiment 9 for MIG welding, whereas it is 4 for TIG welding. For MIG welding, the optimum parameters are: 155 Amp electric current, 11 ft/min feed rate and 20 lit/min gas flow. For TIG welding, the optimum parameters are: 225 Amp electric current and 6 lit/min gas flow. The Taguchi's approach uses the orthogonal array to study large number of design variables by performing minimum number of experiments. The prediction methodology adopted in this paper is quite simple and useful in the Taguchi's design of experiments. The estimates of the UTS for MIG and TIG weld joints is improved by introducing suitably the fictitious input parameters without changing the test runs. Test results are found to be within the expected range of the UTS values for both MIG and TIG weld joints.

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