
Study of relationship between flotation rate and bubble surface area flux using bubble-particle attachment efficiency

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Abstract: Understanding the attachment micro process is a fundamental step toward predicting the rate constant of flotation kinetics. In this research, the effect of bubble-particle attachment efficiency on $k-S_b$ relationship was investigated under Yoon, Stokes and Potential conditions. Maximum Stokes attachment efficiency obtained was 55.9% with particle size of $-37\ \mu\text{m}$, S_b of $34.2\ 1/\text{s}$ and flotation rate of $1.65\ 1/\text{min}$. Stokes attachment efficiency was less than Yoon efficiency and it seems to be a suitable equation for predicting attachment efficiency. Furthermore, three different models were obtained for estimating attachment efficiency using $k-S_b$ relationship.

Keywords: Flotation, Kinetics, Bubble, Attachment

1. Introduction

The bubble-particle collision micro process, attachment and detachment strongly depend on the chemistry and physical chemistry of the surface of solid particle and bubble. At present these two micro processes are the least quantified, because there are many complex phenomena involved which are not well understood yet [1].

Froth flotation is widely used for separating different minerals from each other. However, its influence is limited to a relatively narrow particle size range of $10\text{--}100\ \mu\text{m}$ [2, 3]. Although the effect of particle size on flotation performance has been widely studied to date [2, 4-6], and many important physico-chemical factors related to particle size have been identified, the net effect of these factors are very difficult to predict. For example, in bubble-particle interaction, particle size is known to play a critical role in the probability of particles colliding with bubbles, attachment of particles to bubbles after collision, as well as remaining attached in the pulp [7, 8].

Fine particles typically show slow recovery rates, owing to decreased particle-bubble collisions, and are prone to entrainment. Moreover, very small particles tend to have large specific areas, which can lead to excessive adsorption of reagents, and other effects associated with chemically

active particles. These factors can have a considerable impact on grades and recoveries, depending on the dominant effects in operation [9, 10]. Efficiency of the bubble-particle stability depends on the particle size, particle hydrophobicity and external detaching forces. Even in the flotation of fine particles, the bubble-particle detachment can significantly influence the kinetics of flotation taking place in mechanical cells by intensive turbulent agitation [11]. For these fine particles, the bubble-particle detachment is often neglected. So far the effect of hydrodynamic parameters on flotation response of coarse and fine particles has been widely investigated [12-18].

The surface area flux work has been published in a series of papers [19-24] and Gorain et al (1997) investigated the effect of gas dispersion properties on the flotation rate constant in plant and pilot scale mechanical cells over a range of operating conditions for four impeller types. They found that the rate constant was not readily related to the bubble size, gas holdup or superficial gas rate individually, but it was related to bubble surface area flux (s_b). For example, for shallow froths the relationship was linear [23]. These authors found [23, 24] that s_b (1/s) was strongly related with k (1/min) and that the relationship was linear, as represented by following equation:

$$k = P \times S_b \quad (1)$$

Where P summarized the operational and chemical factors. This k - S_b relationship appears to be independent of both the type and size of mechanical cell and, consequently, has important implications with regard to the optimization, scale-up and design of mechanical flotation cells.

In this research, the effect of bubble surface area flux on bubble-particle attachment efficiency was investigated and bubble-particle attachment efficiency was calculated under Yoon, Stokes and Potential conditions. Furthermore, three models were obtained for estimating bubble-particle attachment efficiency with k - S_b relationship in different conditions. According to author's knowledge, these models are the first equations for predicting bubble-particle attachment efficiency with k - S_b relationship.

2. Materials and Methods

Flotation tests were carried out in a mechanical laboratory

Table 1. Flotation tests conditions

Gas aflow Rate (l/hr)	60				120				180				240			
Impeller Speed (rpm)	900	1000	1100	1200	900	1000	1100	1200	900	1000	1100	1200	900	1000	1100	1200
d_b (μm)	829	752	686	628	826	749	683	625	824	747	681	624	823	746	680	623
ϵ_g (%)	2.86	3.75	4.75	5.87	3.62	4.71	5.93	7.30	4.08	5.29	6.65	8.17	4.48	5.79	7.27	8.92
J_g (cm/s)	0.1	0.1	0.1	0.1	0.2	0.2	0.2	0.2	0.3	0.3	0.3	0.3	0.4	0.4	0.4	0.4
S_b (1/s), Eq. (14)	10.21	10.88	11.53	12.16	16.77	17.94	19.08	20.19	22.69	24.31	25.89	27.43	28.23	30.28	32.27	34.2
V_b (m/s)	0.37	0.31	0.25	0.21	0.37	0.30	0.25	0.21	0.37	0.30	0.25	0.21	0.37	0.30	0.25	0.21
Re_b	307	229	174	133	303	226	171	131	301	224	170	130	299	223	169	130
\mathcal{E} (W/kg), Energy dissipation	2.15	2.95	4.18	5.98	2.15	2.95	4.18	5.98	2.15	2.95	4.18	5.98	2.15	2.95	4.18	5.98

$$\frac{dC}{dt} = -kC \quad (2)$$

Where C is the particle concentration in mass per unit volume and k is a 'rate constant'. The flotation rate constant was calculated assuming the first order rate equation for a batch cell, $R = R_\infty(1 - \exp(-kt))$, and plotting $\ln(1 - R/R_\infty)$ versus t.

The bubble size distribution was measured in a device similar to the McGill bubble viewer. It consisted of a sampling tube attached to a viewing chamber with a window inclined 15o from vertical. The closed assembly was filled with water of a similar nature to that in the flotation cell (to limit changes in bubble environment during sampling) and the tube was immersed in the desired location below the froth. Bubbles rose into the viewing chamber and were imaged by a digital camera as they slid up the inclined window, which was illuminated from behind. In this research, at first, frother was added to the water of the cell and then the viewing chamber was filled with water of the cell to prevent bubble coalescence [25].

The Washburn method was used to measure contact angle on powder. Contact angle of quartz particles was measured

flotation cell. Impeller diameter was 0.07 meter for a cell with square section of 0.13 and height of 0.12 meter. Impeller rotating speed was 900, 1000, 1100 and 1200 rpm and air flow rate was 60, 120, 180 and 240 l/hr. Quartz particles (specific gravity=2.65 g/cm³) of four size classes contain -37, -53+37, -75+53 and -106+75 μm were used for flotation experiments (all size fractions were combined together before flotation). The frother was MIBC (methyl iso-butyl carbinol) with concentration of 22.4 ppm and CCC200 (critical coalescence concentration). The flotation experiments were carried out by dodecylamine collector (50 g/ton) at the natural pH of 8.5 using local tap water. When S_b values were set, all the size fractions floated together under those exact conditions (Table 1).

The air flow rate and impeller speed were set and float product collected at time intervals 1, 2, 3 and 5 minutes. The recovery R determined as a function of time t and flotation rate constant was calculated. The batch wise flotation of mineral particles may be described by a first order rate equation where the rate of removal of particles is given by:

using LAUDA tensiometer (TE3) after flotation tests. The LAUDA tensiometer simplifies the characterization of wetting behavior of the whole surface. The contact angle was measured by means of the precise adjustment of the immersion/ receding rate and micrometer-accurate measurement of the immersion dept. Contact angle of the quartz samples after flotation was obtained 89.7o using this method.

3. Theory

The flotation rate constant is proportional to the collection efficiency [26], this equation can be seen as the embryonic form of the below equation:

$$E_{col} = E_c E_a \quad (3)$$

where E_c is 'the ratio of the number of the particles encountering a bubble per unit time to the number of the particles approaching the bubble at a great distance in a flow tube with a cross-sectional area equal to the projected area of the bubble' [27]. E_a is the attachment efficiency. When the detachment of the attached particles from the bubble surface is considered, Eq. (3) becomes

$$E_{col} = E_c E_a (1 - E_d) \quad (4)$$

Where E_d is the particle-bubble detachment efficiency [28]. The availability of stream function also makes it possible to predict E_a . For predicting attachment probability under Yoon conditions, can use bellow equation [29]:

$$E_a = \sin^2 \left[2 \arctan \exp \left(\frac{-(45 + 8 \text{Re}_b^{0.72}) v t_i}{15 d_b (d_b/d_p + 1)} \right) \right] \quad (5)$$

Where: d_p is the diameter of particle, d_b is the diameter of bubble, t_i is induction time, V is bubble raise velocity. There is another generalized equation for calculation E_a according to [1]:

$$E_a = \text{sech}^2 \left(\frac{2UA t_i}{d_p + d_b} \right) \quad (6)$$

Where: d_p is the diameter of particle, d_b is the diameter of bubble, t_i is induction time, U is particle settling velocity and A is a dimensionless parameter under Stokes flow (A_1) or Potential flow (A_2) according below equations:

$$A_1 = \frac{V}{U} + 1 - \frac{3}{4} \left(1 + \frac{d_p}{d_b} \right)^{-1} - \frac{1}{4} \left(1 + \frac{d_p}{d_b} \right)^{-3} \quad (7)$$

$$A_2 = \frac{V}{U} + 1 + \frac{1}{2} \left(1 + \frac{d_p}{d_b} \right)^{-3} \quad (8)$$

Since d_b , V , U and t_i are four necessary parameters for calculating attachment efficiency, they were obtained using following equations. The mean bubble diameter adopted was the Sauter diameter, calculated by below equation [30]:

$$d_b \text{ or } d_{32} = \frac{\sum n_i d_i^3}{\sum n_i d_i^2} \quad (9)$$

Where n is the number of bubbles, and d is the bubble diameter. If the surface of a drop or bubble is immobile for any reason, the floating velocity is the same as that of a solid sphere and the bubble raise velocity can be described by Stokes' equation [31]:

$$V = \frac{d_b^2}{18\nu} g \quad (10)$$

Where ν is the kinematic viscosity. Also, Particle settling velocity can be described by below equation [32]:

$$U = \sqrt{\frac{3g(\rho_p - \rho)d_p}{\rho}} \quad (11)$$

Where g , ρ_p and ρ are gravitational acceleration, particle density and fluid density respectively. The induction time is a function of the particle size and contact angle which can be determined by experiment and correlated in the form of [33]:

$$t_i = A d_p^B \quad (12)$$

Where parameters A and B are independent of particle size. It was found that parameter B is constant with a value of

0.6, and parameter A is inversely proportional to the particle contact angle θ . Based on these findings, the following equation was used [34]:

$$t_i = \frac{75}{\theta} d_p^{0.6} \quad (13)$$

Where: t_i is given in second, θ in degrees and d_p in meter. The probability of adhesion can now be calculated for given values of bubble size, particle size and contact angle.

4. Results and Discussions

4.1. Bubble Diameter

Bubble diameter was measured. According to Table 1, bubble diameter was 623 to 829 micron. Maximum bubble diameter obtained was 829 micron when impeller speed, air flow rate and bubble surface area flux were 900 rpm, 60 l/hr and 10.21 l/s, respectively. Minimum bubble diameter obtained was 623 micron with impeller speed of 1200 rpm, air flow rate of 240 l/hr and bubble surface area flux of 34.2 l/s. Flotation rate increased with decreasing bubble diameter due to increasing bubble-particle collision efficiency.

4.2. Bubble Surface Area Flux

Calculating S_b in flotation cells is difficult and expensive due to difficulty in measuring bubble diameter. In this research, an empirical model was obtained for estimating S_b in different operating conditions (under conditions of Table 1 with impeller diameter of 0.07 and 0.09 meter and pulp density up to 20%). Impeller peripheral speed (N_s) instead of impeller speed (N) was used to determine the contemporary influence of impeller speed and impeller diameter in models. Also, superficial gas velocity (J_g) instead of air flow rate per unit cell cross-sectional area (Q/A) was used for modeling. P_d is pulp density.

$$S_b = 25 N_s^{0.699} J_g^{0.805} P_d^{0.005} \quad R^2=0.92 \quad (14)$$

4.3. k - S_b Relationship

According to Fig. 1, flotation rate increased with increasing bubble surface area flux and decreasing particle size. When particle size, impeller speed and bubble surface area flux were 37 μm , 1100 rpm and 32.27 l/s, maximum flotation rate was obtained 1.89 l/min. coarser quartz particles showed a pronounced lower flotation rate than finer ones. It seems that bigger particles demand much more turbulence to become suspended and collide with air bubbles than smaller ones.

A deviation is observed from linear k - S_b relationship in Fig. 1. This could be due to the inapplicability of the hypothesis by Gorain et al. (1997) of linear k - S_b relationship. So, a $k = P \times S_b^\alpha$ relationship was assumed for flotation response of quartz particles and a model was fitted to actual values for obtaining influence of particle size on k - S_b relationship. Eq. (15) explains the effect of particle size in P and α constants.

$$k = 0.057d_p^{-0.075} \times S_b^{\exp(-0.059/d_p)} \quad R^2=0.71 \quad (15)$$

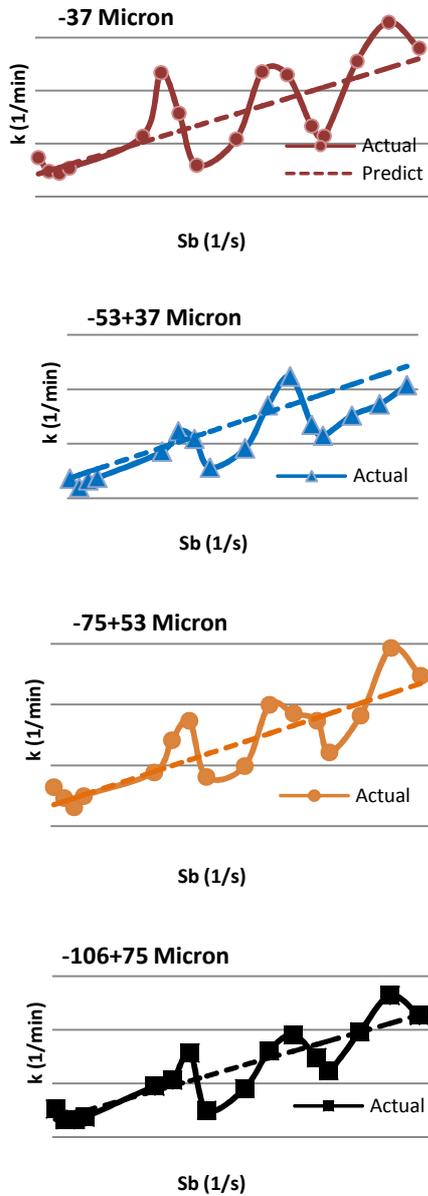


Fig. 1. k - S_b relationship for different particle sizes

4.4. Calculating Attachment Efficiency

According to Fig. 2a, Yoon attachment efficiency was calculated for different particle sizes using Eq. (5). In this research, with decreasing particle size, attachment efficiency increased to maximum magnitude of 94.8%. With increasing S_b , flotation rate increased but attachment efficiency decreased. So, increasing flotation rate can be attributed to increasing collision efficiency.

According to Fig. 2b, Stokes attachment efficiency was calculated for different particle sizes using Eqs. (6,7). Minimum attachment efficiency obtained was 1.9% with particle size of -106+75 μm , S_b of 10.21 1/sec and flotation rate of 0.41 1/min and maximum attachment

efficiency obtained was 55.9% with particle size of -37 μm , S_b of 34.2 1/s and flotation rate of 1.65 1/min. Stokes attachment efficiency was less than Yoon efficiency.

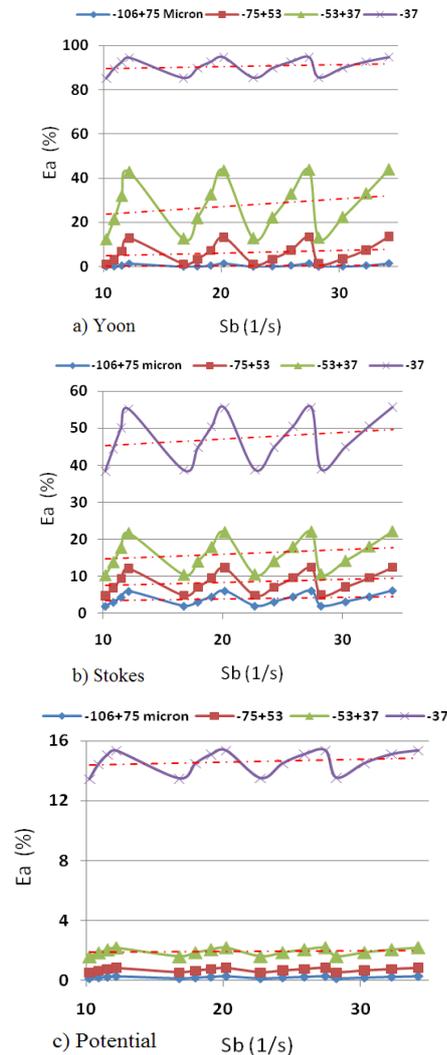


Fig. 2. Attachment efficiency under Yoon, Stokes and Potential flow conditions (particle density of 2.65 g/cm^3 and contact angle of 89.7°)

According to Fig. 2c, Potential attachment efficiency was calculated for different particle sizes using Eqs. (6,8). Maximum attachment efficiency obtained was 15.5% with particle size of -37 μm , S_b of 34.2 1/s and flotation rate of 1.65 1/min. Attachment efficiency calculated by Potential flow conditions was very lower than both Yoon and Stokes attachment efficiencies. So, Potential efficiency was not a suitable equation for predicting attachment efficiency under conditions of this research (laboratory mechanical flotation cells). Stokes attachment efficiency was between Yoon and Potential attachment efficiency.

4.5. Primary Predicting of Bubble- Particle Attachment Efficiency Using k - S_b Relationship

Three different models were obtained for estimating attachment efficiency using k - S_b relationship. All of four particle size classes (-37, -53+37, -75+53 and -106+75 μm)

were used for this purpose. Different forms of multiple regression models (exponential, linear, polynomial and power) were examined by comparing their statistical significance using coefficient of multiple determinations (R^2) and following models were obtained for $10.21 < S_b < 34.2$ 1/s and $0.32 < k < 1.89$ 1/min. So, following equations explain influence of Yoon (E_{a-Y}), Stokes (E_{a-S}) and Potential (E_{a-P}) attachment efficiency on $k-S_b$ relationship for different particle size fractions. N is data numbers of the each model. The effect of $k-S_b$ relationship on attachment efficiency has been illustrated in Fig. 3.

equations can be used only for small particles ($< 53 \mu\text{m}$).

$$E_{a-Y} = 7.76 \times 10^{-4} t_i^{-1.632} \left(\frac{k}{S_b}\right)^{-0.137} \quad (16)$$

$$E_{a-S} = 10.59 \times 10^{-4} t_i^{-1.488} \left(\frac{k}{S_b}\right)^{-0.145} \quad (17)$$

$$E_{a-P} = 0.013 \times 10^{-4} t_i^{-2.336} \left(\frac{k}{S_b}\right)^{-0.026} \quad (18)$$

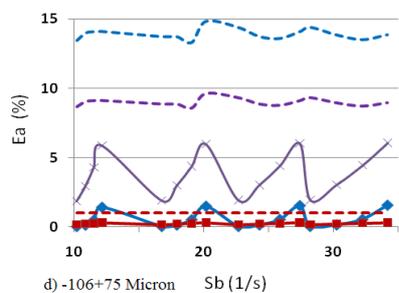
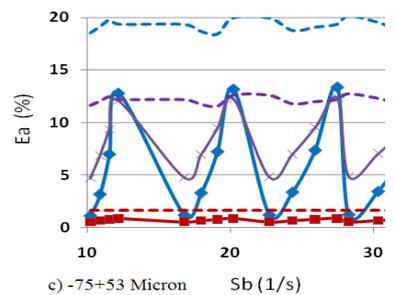
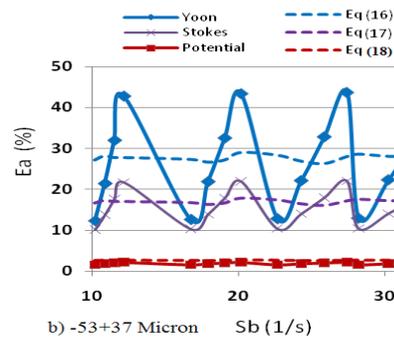
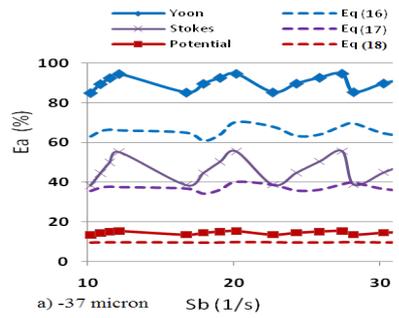
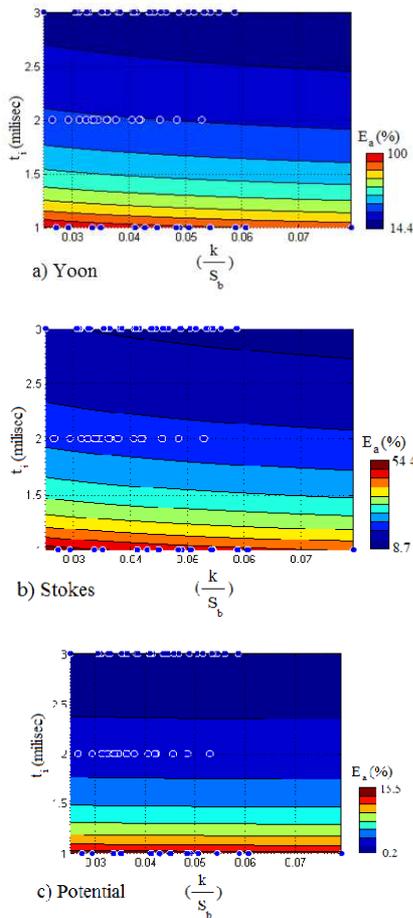


Fig. 3. Predicting bubble-particle attachment using $k-S_b$ relationship (particle density of 2.65 g/cm^3 and particle size of < 106 micro meters)

Fig. 4. Compares bubble-particle attachment calculated using different equations. According to Figs. (4a, 4b), for particle size of -37 and $-53+37 \mu\text{m}$, below equations can be useful for estimating Yoon, Stokes and Potential attachment efficiency and equivalent plots are compatible together.

According to Figs. (4c, 4d), for particle size of $-75+53$ and $-106+75 \mu\text{m}$, following equations are not suitable for predicting attachment efficiency because the equivalent plots are not compatible together. It can be attributed to high efficiency of bubble-particle collision and detachment. Bubble-particle collision and detachment efficiency of coarse particles are effective on the flotation rate too. So, below

Fig. 4. Comparing bubble-particle attachment calculated using different equations (particle density of 2.65 g/cm^3 and contact angle of 89.7°)

5. Conclusions

In this research, the effect of $k-S_b$ relationship on bubble-particle attachment efficiency was investigated under Yoon, Stokes and Potential conditions and following conclusions were illustrated:

Attachment efficiency calculated under Yoon conditions was more than Stokes and Potential efficiency. Maximum Stokes attachment efficiency obtained was 55.9% with particle size of $-37 \mu\text{m}$, S_b of 34.2 1/s and flotation rate of 1.65 1/min. Maximum Potential attachment efficiency obtained was 15.5% with particle size of $-37 \mu\text{m}$, S_b of 34.2 1/s and flotation rate of 1.65 1/min. Attachment efficiency calculated by Potential flow conditions was very lower than both Yoon and Stokes attachment efficiency. Also, three different models were obtained for estimating attachment efficiency using $k-S_b$ relationship.

Nomenclature

A	Unit cell cross sectional area	N	Impeller speed
C	Concentration	N_s	Impeller peripheral speed
CCC	Critical coalescence concentration	P_d	Pulp density
d_b	Bubble diameter	Q	Air flow rate
d_p	Particle size	Re_b	Bubble Reynolds number
E_a	Attachment efficiency	R	Recovery
g	Acceleration due to gravity	R_∞	Infinite recovery
J_g	Superficial gas velocity	S_b	Bubble surface area flux
k	Flotation rate constant	t_i	Induction time
E_c	Collision efficiency	ν	Kinematic viscosity
E_{col}	Collection efficiency	ϵ	Energy dissipation
E_d	Detachment efficiency	θ	Contact angle

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