

Research Article

Hubble Diagram Test of SN1a Supernovae and High Redshift Gamma Ray Bursts

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Abstract

Hubble diagrams are examined for SN1a supernovae in the redshift range $z = 0.01$ – 1.3 and for gamma ray bursts in the range $z = 0.034$ – 8.1 . It is shown that in the low redshift range, the Hubble diagram shows an innate equivocality between the Λ CDM and the tired light model. This means that the strong agreement between the z/μ data, calculated with the parameters of the Λ CDM model, and the experimentally measured z/μ values cannot be considered as definite evidence for the expansion hypothesis. The exponential function $z+1 = e^{h(TL) \times t(d)}$ which is characteristic of the tired light redshift mechanism, fits the data with similarly high accuracy. Hence, on the premise of low redshift data, a decision for or against either model is completely arbitrary. We expect that in the high RS range it should be possible to check more precisely whether the HD follows the linear $H_0 D/c$ or the exponential relation, an effect that is not perceptible in the $z < 1$ region. Unfortunately, SN1a supernovae data are accessible only to a limited range of distances. This constraints on the data motivated several attempts to obtain cosmological parameters from gamma ray bursts observations. GRBs are the most brilliant sources in the universe. They are acquired up to RSs of ~ 8 and higher, and endeavours are made to use GRB data to calculate HD. In this study a total of 138 calibrated, cosmology independent GRB z/μ data points collected by Liu and Wei from the 557 Union2 compilations were used as the starting data set. It is shown that the Hubble diagram for high redshift gamma ray bursts shows poor agreement with the Λ CDM model, but concurs with the exponential energy decay following from the tired light hypothesis.

Keywords

Distances and Redshifts, Galaxies, High-redshift, Gamma Ray Bursts, Cosmological Parameters

1. Introduction

The essential premise of Big Bang (BB) cosmology is that the universe is expanding, and Hubble's law, Hubble [1], is viewed as the most persuasive proof for cosmic expansion. In present-day cosmology, the velocity interpretation of the redshift (RS) of spectral lines has achieved a dogmatic status, and objections against it have gone unobserved.

Regardless of whether this interpretation is correct or not,

Hubble's law is a RS/distance (d) relation, and an interpretation of this as a velocity is only a hypothesis. Supporting the velocity interpretation is the good agreement between the observed z/μ data for SN1a supernovae in the RS range $z < \sim 1.3$ with data determined based on the parameters Ω_M , Ω_Λ , w and H_0 of the Λ CDM model, which is viewed as proof for general expansion. Despite its widespread acceptance, however, this conclusion is equivocal, and the current circum-

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stance is fairly confounding. Based on a semiquantitative examination of SN1a data Sorell [2] reported that in the low-RS range, the Hubble diagram (HD) for a tired light (TL) cosmology gives good agreement with the Type Ia supernova data. A detailed examination of mixed SN1a and gamma ray burst (GRB) data Marosi [3] has also shown that in the RS range 0.031–8.1, the TL model, Zwicky [4], closely fits the experimental data, while the Λ CDM model is in poor agreement with observation. A comparable outcome was described by Traunmüller [5], whose examination of 892 SN1a supernovae z/μ data also indicated that these were well-matched with the TL model.

The interpretation of the RS of atomic spectral lines suffers from the fact that none of the proposed systems (the expanding space paradigm or the TL mechanism) can be confirmed experimentally, meaning that confidence in each hypothesis should be estimated based on its ability to explain the observational data. One important issue in cosmology is therefore to explain which of the two models fits the observed data better, i.e., whether the HD follows the linear (expanding universe) or the exponential TL relation. In the high RS range, it should be more feasible to check more precisely whether the HD follows a linear or exponential slope.

Very exact z/μ data for SN1a supernovae, however, are accessible only for a limited range of distances. At $RS > \sim 1.3$, the optical light emitted by a supernova gradually diminishes with distance, making definite estimations difficult. Hence, some attempts have been made to collect and use GRB data for computing HDs in the high RS range, Schäfer [6, 7], Wei [8], Amati [9].

Using mixed SN1a and GRB or exclusively GRB data, Marosi [10–12] observed that the slope of the HD is (or is extremely close to) exponential, which is characteristic of the TL model. In contrast, ongoing investigations by Gupta [13] and Shirokov et al. [14, 15] have found that although none of the existing studies has given probative affirmation for the Λ CDM model, the conclusion can be drawn that based on the HD test, the TL model can be precluded. This cosmologically significant inconsistency between these two contradictory conclusions requires an amendment.

2. Aims

The HD test represents possibly the most significant proof for identifying the underlying physical nature of the Hubble constant (abbreviated as $h^{\text{CDM}} = (\text{km s}^{-1} \text{ Mpc}^{-1})/100$ for Λ CDM and $h^{\text{TL}} = (\text{Hz s}^{-1} \text{ Hz}^{-1})/100$ for the TL model), and could provide solid support for the expansion hypothesis, or, in the contrary case, for the legitimacy of the TL model (although this would require modification to the Λ CDM itself).

The aim of the present study was to perform a comparative HD test using cosmology-independent SN1a data and high RS GRB RS/μ data. Since both the Λ CDM and the TL model make precise forecasts about the shape of the HD, it ought to

be possible to confirm whether the HD shows a linear

$$z = h_0 \times t(d) \quad (1)$$

or exponential relationship

$$z + 1 = e^{h^{\text{TL}} \times t(d)} \quad (2)$$

where t represents the flight time of the photons from the co-moving radial distance d to the observer; for simplicity, we will use t instead of d in the following discussion). This could set significant constraints on these contrasting cosmological models.

We do not plan to examine existing issues related to the Λ CDM and TL cosmology, or to accept or reject either model on the basis of hypothetical contentions or hypotheses. The present study is completely cosmology-independent; it is a mathematically based statistical investigation based on cosmology-independent data without the need to turn to cosmological suspicions, meaning that it is unbiased.

3. Datasets and Methods

3.1. SN1a Supernovae

(a) For the model calculations, the cosmological parameters $\Omega_M = 0.295$, $\Omega_\Lambda = 0.705$, $w = -1.018$ and $h_0 = 0.7$ were used, based on 374 spectroscopically affirmed, upgraded SN1a supernovae from the most recent joint light-curve analysis (JLA) data index, Betoule et al. [16].

3.2. Choice of GRB Data

(b) 60 low RS and 78 high RS GRB data samples from the Union1 compilation, collected by Liu and Wei [17]. One extreme outlier at $\ln(z+1) = 1.2095$ with $t = 17491 \times 10^{-14}$ was excluded from the calculation.

(c) 193 GRB data samples collected by Amati et al. [9].

(d) 134 GRB data samples, Demianski [18].

A comparison of the goodness of fit indicators for data sets b), c) and d) is shown in Table 1.

Table 1. Descriptive statistics from the considered GRB data sets.

Data set	(b)	(c)	(d)
No. of data points	138	193	134
z range	0.031–8.1	0.03354–8.1	1.48–9.3
Data points $z \geq 5$	6	5	5
R^2	0.8746	0.7848	0.8241
$\sum \chi^2$ (best fit: obs)	1.9193	5.1282	2.8849

Data set	(b)	(c)	(d)
$\sum \chi^2/\text{data point}$	0.0139	0.02657	0.02153
Standard deviation	2.196	2.2256	2.2623

Based on the above quality criteria, we selected 138 calibrated, cosmology-independent GRB data points in the RS range $z = 0.0331\text{--}8.1$ for a detailed analysis.

4. Data Processing

Data were introduced on the usual, strongly attenuated logarithmic z/μ scale, and since the contrast between the measured and the modelled data turned out to be clearer on the linear scale, we also considered the less commonly used but more sensitive linear photon flight time $t/(z+1)$ scale. A conspicuous benefit of the $t/(z+1)$ representation is the direct illustration of the shape of the HD, which can be definitively contrasted with the expectations following from Equations (1) and (2).

4.1. Data Conversion from μ to $t(d)$ and Vice Versa

For data conversion from μ to t we used Equation (3), and for conversion from t to μ we used Equations (4) and (5), as follows:

$$t = \frac{D}{c} = \frac{10^{(\mu+5)/5}}{(z+1) \times 3 \times 10^{10}} \times 3,0857 \times 10^{18} \quad (3)$$

$$x = \frac{t}{3,0857 \times 10^{18}} \times (z+1) \times 3 \times 10^{10} \quad (4)$$

$$\mu = (\log(x) \times 5) - 5 \quad (5)$$

Conversion of the SN1a μ data to a linear scale was straightforward, as the data were of high precision and Equation (3) could directly be applied for conversion without producing disruptive amplification of measurement errors.

Due to experimental difficulties in determining z/μ data at high RS, these data were overwhelmed by substantial scatter, meaning that they could not be converted to the linear $t/(z+1)$ scale without amplifying the scatter and making the converted data unmanageable. Hence, before data conversion, there was a need to either smooth the data scatter by calculating the line of best fit using a suitable arithmetical function or to multiply the t values by an appropriate damping factor, which in this case was selected as 10-14. For data fitting, a third-order polynomial regression was used.

4.2. Goodness of Fit

The goodness of fit was calculated using the likelihood estimator

$$\chi^2 = \sum_{i=1}^N \frac{(\mu_{obs.} - \mu_{calc.})^2}{\mu_{calc.}} \quad (6)$$

4.3. Calculations of RS/ μ Data

For the Λ CDM model, the ICAR cosmology calculator was used to calculate the theoretical z/μ data. For the TL models, the z/μ data were calculated as follows:

$$\mu = 25 + 5 \times \log(c / H^{TL}) + 5 \times \log(1+z) + 5 \times \log \ln(1+z) \quad (7)$$

(see: Sorrell [2]; Vigoureux, Vigoureux & Langlois [19], Traunmüller [5].)

4.4. Data Presentation

Excel was used for data fitting, refinement, and presentation.

5. Equivocality of the SN1a Supernovae Hubble Diagram

Since for Λ CDM models the distances in Equation (1) are nonlinear in z (the distances are limited by the maximum value for d , i.e., the radius of the universe), it is usual to express d as $d \approx 10^{(\mu+5)/5}$. This leads to a linear relationship for the variables

$$\log(z) \approx \mu \quad (8)$$

which are the usual coordinates for the graphical presentation of the HD.

For TL models, it follows from Equation (2) that

$$\ln(z+1) = h^{TL} \times t \quad (9)$$

which is linear with distance, with an intercept on zero.

Figure 1 shows the HD calculated with the parameters of the Λ CDM model, as set down by Betoule et al. [16], in the RS range $z = 0.01\text{--}1.35$ for the $\log(z)/\mu$ presentation. Figure 2 shows the same data plotted on the $\ln(z+1)/t$ scale.

The fit parameters and goodness of fit indicators are presented in Tables 2 and 3.

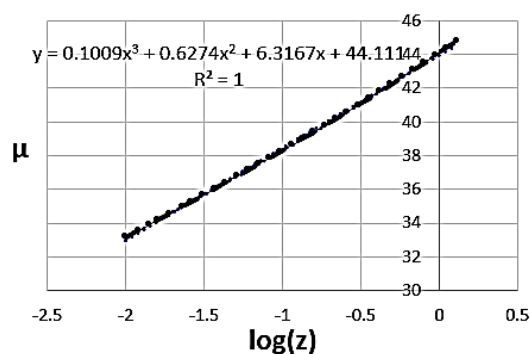


Figure 1. $\log(z)/\mu$ Hubble diagram for the 31 calculated z/μ data points.

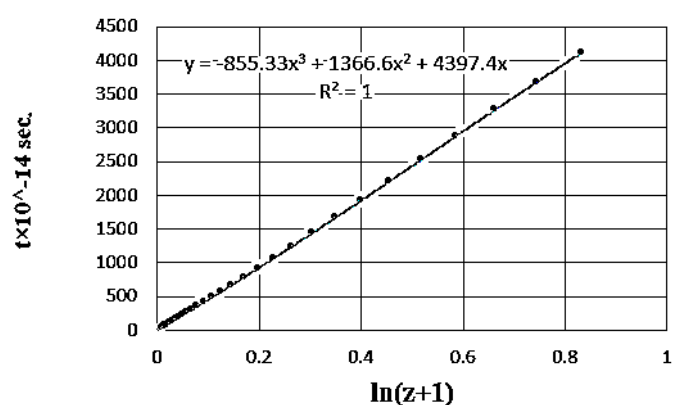


Figure 2. $\ln(z+1)/t$ Hubble diagram for the 31 calculated z/d data points.

Table 2. Fit parameters on the linear $\log(z)/\mu$ and $\ln(z+1)/t$ scales.

	Parameter 1	Parameter 2	Parameter 3	Parameter 0
log fit	0.1009	0.6274	6.3167	44.111
ln fit	-855.33	1366.6	4397.4	0

Table 3. Goodness of fit indicators the linear $\log(z)/\mu$ and $\ln(z+1)/t$ scales.

Fit coordinates	$\sum \chi^2 \mu_{\text{calc}}: \mu \text{ fit}$	R^2	P test	Chiqu-test	F test
$\log(z)/\mu$	2.673×10^{-5}	1	0.9999985	1	0.9987774
$\ln(z+1)/t$	1.810×10^{-6}	1	1	1	0.9987774

As illustrated by **Figures 1 and 2**, both Equation (8) (the expanding universe model) and Equation (9) (the TL model) match the calculated data with very high accuracy. The ex-

ceptionally small $\sum \chi^2$ values on the order of 10^{-5} – 10^{-6} offer convincing evidence of the equivocality of the Λ CDM and TL model in the low RS range.

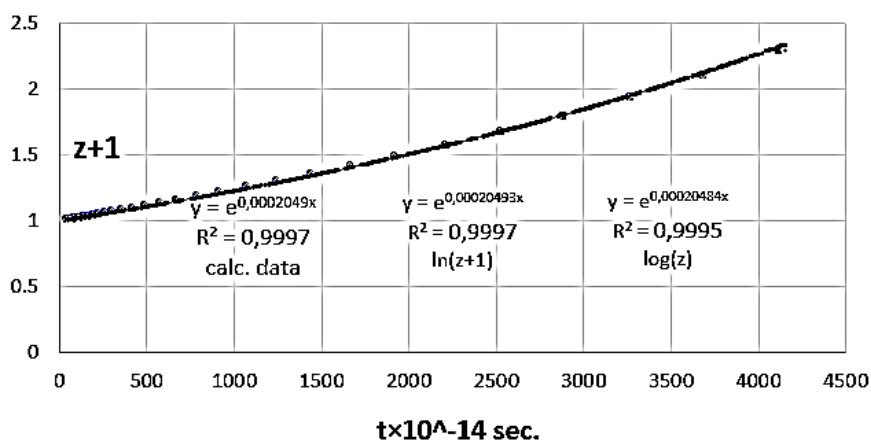


Figure 3. Linear HDs for the calculated data (dots) and for the $\log(z)/\mu$ (triangles) and $d/\ln(z+1)$ (squares) models.

The corresponding linear $t/(z+1)$ HDs were derived by converting μ to t using Equations (3-5) based on the fit coefficients from Equations (8) and (9). The linear HDs for both the $\log(z)$ and the $\ln(z+1)$ representations and the linear HD for the calculated data are shown in Figure 3.

The three curves (i.e., the one calculated based on the parameters of the Λ CDM model, and the $\log(z)/\mu$ and $d/\ln(z+1)$ lines) have an exponential slope, are closely congruent, and cannot be told apart by visual examination. The corresponding Hubble constants and variances are shown in Table 4.

Table 4. Hubble constants and variances for the linear $t/(z+1)$ HD.

Model	Calculated data	ln fit	log fit
h	0.6322	0.6322	0.6319
R ²	0.99967	0.99967	0.99948

The Hubble constants are similar to within 0.5%, with values of $h^{\text{TL}} = 0.6319$ for the logarithmic $\log(z)/\mu$ fit and 0.6322 for the $\ln(z+1)$ fit and calculated data.

Table 6. Comparison of $\sum \chi^2$ values for $h^{\text{CDM}} = 0.70$, $h^{\text{TL}} = 0.70$ and the Best fit $h^{\text{TL}} = 0.66$ with the observed data in the RS range 0.031–8.1.

Model, calc. μ	$h^{\text{CDM}} = 0.70$	$h^{\text{TL}} = 0.66$	$h^{\text{TL}} = 0.70$
$\sum \chi^2 \mu_{\text{obs}}/\mu_{\text{calc}}$	1.9415	1.9397	1.9923

The $\sum \chi^2$ differences between $h^{\text{CDM}} = 0.70$ and $h^{\text{TL}} = 0.70$ for the observed data show that $h^{\text{TL}} = 0.70$ gives the poorest fit, whereas a comparison of $h^{\text{CDM}} = 0.70$ with $h^{\text{TL}} = 0.66$ shows the opposite: the $h^{\text{TL}} = 0.66$ model gives the best fit to the observed data. The use of $h^{\text{TL}} = h^{\text{CDM}}$ instead of the best fit h^{TL} for comparison inevitably leads to the wrong conclusion, that the TL model does not fit the data and can therefore be rejected. The results presented here show that for a proper comparison of $\sum \chi^2$ for TL models, the correct approach is a Hubble constant close to the expectation value of h^{TL} , as shown in Table 5, or, depending on data quality (influence of scatter and/or outliers on χ^2), the best-fit value of h^{TL} .

6. Hubble Diagram for High RS GRBs

6.1. $\log(z)/\mu$ Hubble Diagram

The $\log(z)/\mu$ Hubble diagram is depicted in Figure 4.

Based on model calculations using 35 equidistant data points in the RS range $z = 0.03$ –1.02, the h^{TL} equivalents for $h^{\text{CDM}} = 0.68$, 0.70 and 0.73 were determined in a similar way. The results are summarised in Table 5.

Table 5. Equivalent values for h^{CDM} and h^{TL} .

h^{CDM}	h^{TL}	$h^{\text{TL}}/h^{\text{CDM}}$
73	65.92	0.9031
70	63.22	0.9031
68	61.41	0.9031

An obvious but frequently overlooked outcome is that, as shown in Table 5, the equivalent Hubble constants h^{CDM} and h^{TL} are different, and this has a significant effect on the comparative evaluation of the Λ CDM and TL models in the high RS range. It can be seen from Table 6 that the comparison of the observed high RS GRB data with the competing Λ CDM and TL models using $h^{\text{CDM}} = h^{\text{TL}}$ is imprecise.

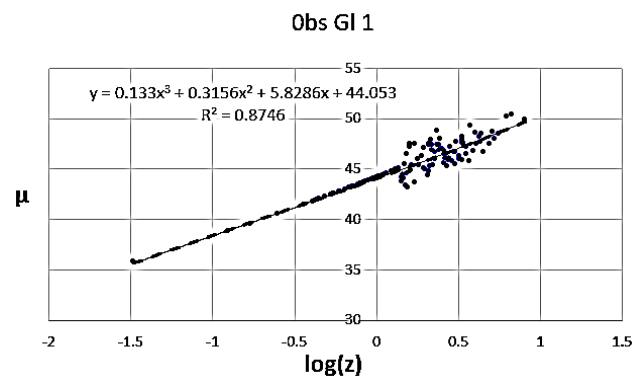


Figure 4. $\log(z)/\mu$ Hubble diagram of the observed GRB data.

As the data points for high RS show pronounced scatter, the variance of the fit reaches only $R^2 = 0.8746$, and cannot be improved by any other reasonable mathematical function. The fit coefficients are shown in Table 7.

Table 7. Fit coefficients for the $\log(z)/\mu$ Hubble diagram.

Parameter 1	Parameter 2	Parameter 3	Parameter 0	R ²
0.133	0.3156	5.8286	44.0533	0.8746

Figure 5 shows the linear $t/(z+1)$ HDs inferred from the best fit coefficients of the observed data (squares) together with the corresponding exponential $h^{\text{TL}} = 0.66$ (dots) and the HD for $h^{\text{CDM}} = 0.70$ (triangles).

$h^{\text{TL}} = 0.66$ (dots).

The GRB HD exhibits some irregular shape between $h^{\text{TL}} = 0.66$ and $h^{\text{CDM}} = 0.7$ with

$$\chi^2 = \sum_{i=1}^N \frac{(\mu_{\text{fit}, \text{obs.}} - \mu_{\text{TL}, \text{calc.}})^2}{\mu_{\text{TL}, \text{calc.}}} = 0.0196, \text{ and}$$

$$\chi^2 = \sum_{i=1}^N \frac{(\mu_{\text{fit}, \text{obs.}} - \mu_{\text{CDM}, \text{calc.}})^2}{\mu_{\text{CDM}, \text{calc.}}} = 0.03028$$

($\mu_{\text{fit}, \text{obs}}$ stands for calculated magnitudes inferred from the polynomial best-fit function, $\mu_{\text{TL}, \text{calc.}}$ and $\mu_{\text{CDM}, \text{calc.}}$ were calculated from $h^{\text{TL}} = 0.66$ for the TL and from $\Omega_{\text{M}} = 0.287$, $w = -1$ and $h^{\text{CDM}} = 0.7$ for the Λ CDM model, respectively.)

The result favours the TL model, but as can be seen from Figure 5, the deviation from the ideal exponential shape is too large to draw safe conclusions. A profile examination shows systematic deviations, especially at $RS \geq 3-4$, where data points are visible above the exponential line.

In summary, the Λ CDM model shows a poorer fit to the HD calculated on the basis of observed data, which suggests a

somewhat better but still not correct portrayal of the TL model. No safe conclusion in favour of or against either of the competing models can be drawn from this result.

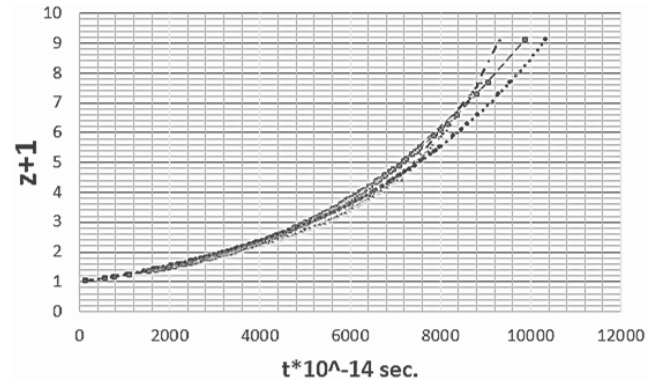


Figure 5. $h^{\text{CDM}} = 0.7$ (triangles), best fit of the observed data (squares).

6.2. $\ln(z+1)/t$ Hubble Diagram

The linear $\ln(z+1)/t$ Hubble diagram is shown in Figure 6.

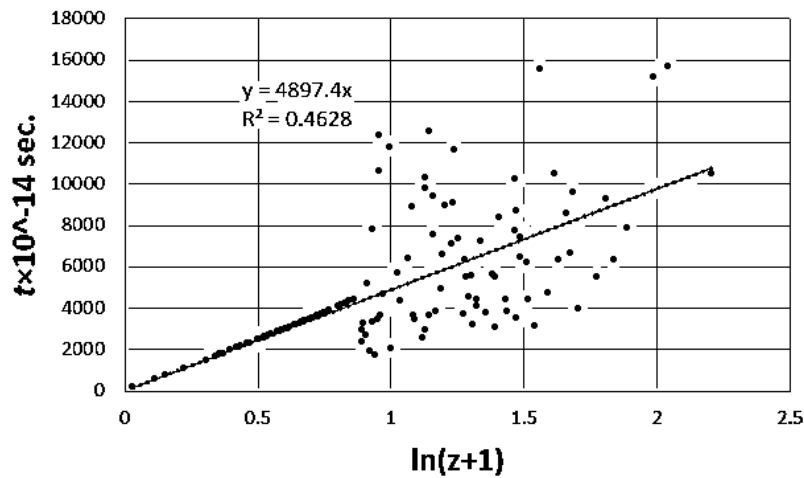


Figure 6. Linear HD on the $t/(z+1)$ scale of the observed GRB data.

Despite the extensive scatter in the observed photon flight times even at values of $z \geq 1.4$, the $\ln(z+1)/t$ diagram is linear.

Considering the quality of the data, it shows an astonishingly good variance of $R^2 = 0.8447$ that could only be worsened by

fitting the observed data with higher-order polynomials. From Figure 6, the equation that describes the photon flight time/ z relationship on the $t \times 10^{-14}$ scale that goes into the linear $t/(z+1)$ diagram is

$$t = 4897 \times \ln(z+1) \quad (10)$$

Figure 7 shows the corresponding $t/\ln(z+1)$ HD.

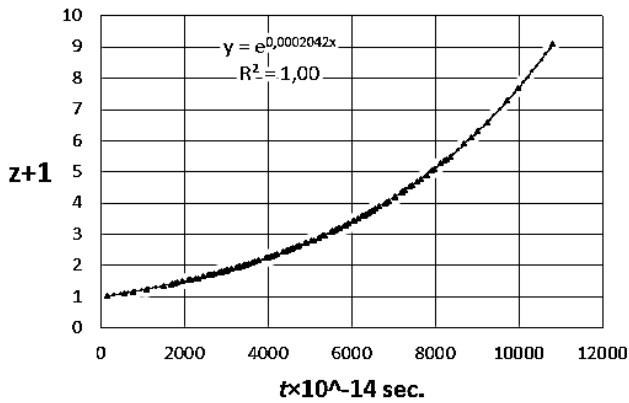


Figure 7. $t/\ln(z+1)$ HD for the observed GRB data.

The linear HD has a perfect exponential slope, with $h^{TL} = 0.63$ in exceptionally good agreement with the expected value of $h^{TL} = 0.632$ obtained from model calculations.

7. Discussion

The results of the $\ln(z+1)/t$ -test show that both the low RS SN1a data and the high RS GRB HDs provide an adequately good exponential fit to the observed z/μ data, which is characteristic of TL cosmology. This finding, in turn, implies a static universe. This result is in clear conflict with the predictions of the currently accepted expanding Λ CDM model, which is incompatible with an exponential slope of the HD in the high RS range. Since expansion cannot be measured experimentally, various tests based on observational data have been proposed to provide evidence for the expansion hypothesis; Sandage et al. [20], Sandage, Perlmutter [21], Sandage, Lubin [22], Hubble, Tolman [23], Alcock, Paczyński [24]: (i) the Tolman surface brightness test, (ii) the time dilation test, (iii) the cosmic microwave background temperature as a function of the RS test, (iv) the apparent magnitude versus distance test, (v) the angular size versus the RS test and, (vi) the Alcock-Paczynski test have been suggested as possible observational evidence for the expanding space hypothesis. The results of these tests indicate that expansion as predicted by the Λ CDM model with $h = 0.7$ can be excluded. Static and slowly expanding universe (SEU) models (La Violette, personal communication) fit the observations more accurately, Lopez-Corredoira [25, 26], Cawford [27],

LaViolette [28], Lerner [29]. Presently, concordance cosmology cannot give convincing explanation to these conflicting results. Uncertainties about the true physical origin of the cosmic redshift, due to expansion or energy loss according to the TL theory, require careful re-evaluation.

8. Uncertainties and Recent Developments

The problem with the Hubble constant is that redshift from local measurements (calculated from the redshift of spectral lines emitted by distant galaxies) and redshift from global measurements (calculated from the CMB power spectrum) lead to different results: H_0 (local) = $72-73 \text{ km s}^{-1} \text{ Mpc}^{-1}$ as compared to H_0 (global) = $67.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The significant difference between the local and global measurements is taken so seriously that the need for new physics beyond the current standard model has been discussed in order to explain this discrepancy. Attempts to bring together these two values have been unsuccessful.

A further problem concerns the age of the universe. Recently, the JWST has discovered galaxies appearing older than the universe itself, Gupta [30]. Both problems are tightly bound not only to the value but also to the physical nature of the Hubble constant.

Since it cannot be excluded that due to systematic errors in distance (D) calculations, for example, the magnitude/redshift relation that is essential for the construction of the HD, may be subject to unidentified systematic errors, it is important to have different methods which may not be subject to the same sources of errors. Various fundamentally different methods have been employed determine the accurate value of the Hubble constant such as estimating the Hubble constant with gravitational waves [31, 32] and the four - parameter χ^2 -Test [33, 34]. However, these methods have not yet been systematically tested and quantitative comparison with results obtained by other methods is lacking.

9. Conclusions

The most significant conclusion of the HD test introduced in this analysis is that within the low RS range of $z = 0.01-1.3$, the HD is equivocal and permits no distinction between the Λ CDM and TL models. The HD can be equally well described by the parameters of the Λ CDM model as by the exponential function $z+1 = e^{h^{TL} \times t(d)}$

In the high RS range up to $z = 8.1$, the observed z/μ data conflict with the Λ CDM model, and exhibits an exponential slope. This result contradicts many established facts and theories about the universe. Such a significant discrepancy regarding one of the most important cosmological parameters, however, requires further clarification.

Abbreviations

H_0	70 km Mpc ⁻¹ s ⁻¹
h	$H_0/100$ km Mpc ⁻¹ s ⁻¹ = 0.7
HD	Hubble Diagram
RS	Redshift
GRB	Gamma Ray Burst

Author Contributions

Laszlo Arpad Marosi is the sole author. The author read and approved the final manuscript.

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Data Availability Statement

The author confirms that the data supporting the findings of this study are available within the article and the reference list.

Conflicts of Interest

The author declares no conflict of interest.

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